



**Vamos a comenzar en breve, a las 1 CDT / 2 EDT**

## Cómputo Cuántico para Química



El cómputo cuántico es una de las áreas de expansión prometedora para la química teórica. Las computadoras cuánticas usan efectos cuánticos para realizar procesos de cómputo. Este nuevo tipo de computadora puede simular a los átomos y a las moléculas, así como a los materiales de manera exacta.

En esta presentación, el Dr. Alán Aspuru-Guzik Profesor de Química y de Ciencias de Computación en la Universidad de Toronto describirá qué es el cómputo cuántico, cuál es el estado actual del campo y algoritmos y experimentos que recientemente se han realizado en estas computadoras.

### Lo Que El Público Aprenderá

- Qué son las computadoras cuánticas
- Por qué las computadoras cuánticas prometen ser una herramienta valiosa para las ciencias químicas
- El estado actual del cómputo cuántico para la química

### Ponente y Moderadora



Alán Aspuru-Guzik  
Universidad de  
Toronto



Ingrid Montes  
Universidad de  
Puerto Rico, Recinto  
de Río

### *El Vigésimo Webinar en Español auspiciado por ACS y SQM*

<http://bit.ly/ComputoCuantico>

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### ¿Tiene preguntas para el ponente?



### “¿Por qué he sido “silenciado”?

No se preocupe. Todo el mundo ha sido silenciado, excepto el ponente y la moderadora. Gracias, y disfruten de la presentación.

**Escriba y someta sus preguntas durante la presentación**

2



¿Está en un grupo hoy viendo el webinar en vivo?



Díganos de dónde son ustedes y cuántas personas están en su grupo!

3



### La Diversidad de la Audiencia



Hoy tenemos representantes de **24 países**

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## ¡C&EN en Español!

C&EN pone a su disposición traducciones al español de sus artículos más populares.

August 14, 2018

**La FDA aprueba la primera terapia con ARN interferente**  
El staff de OnPatro pone fin a dos décadas de trabajo académico e industrial para llevar los ARN interferentes al mercado farmacéutico.



July 31, 2018

**El óxido nítrico del permafrost tibetano esconde malas noticias para el calentamiento global**  
Los científicos estiman que el deshielo podría liberar grandes cantidades de este gas de efecto invernadero.



July 25, 2018

**Peces sin olfato en los océanos acidificados**  
Los crecientes niveles de CO<sub>2</sub> podrían impedir que los peces encuentren comida o detecten sus depredadores.



Gracias a una colaboración con la organización española Divulgame.org, C&EN ahora es capaz de ofrecer traducciones al español de algunos de nuestros mejores contenidos. Queremos hacer de la ciencia de vanguardia más accesible a la comunidad química de habla española, y esta es nuestra contribución. Le da a los nacidos en España, América Latina, o los EE.UU., pero cuyo primer idioma es el español la oportunidad de leer este contenido en su lengua materna. Esperamos que les guste y sea de su utilidad.



**Dr. Bibiana Campos Seijo**  
Editora en Jefe, C&EN

<http://bit.ly/CENespanol>

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## Sociedad Química de México



Desde sus comienzos de la Sociedad Química de México, se buscaba un emblema sencillo, no demostrar partidarismo alguno y significar al gremio, debería representar un símbolo no sólo para los químicos, sino también para ingenieros, farmacéuticos, metalurgistas, en fin que englobe e identifique por igual a los científicos en todas sus áreas de las ciencias químicas.

[www.sqm.org.mx](http://www.sqm.org.mx)

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## ¡El Próximo Webinar de 2018!

**Miércoles, el 17 de Octubre**

*“El Reto de la Terapia Antioxidante”*



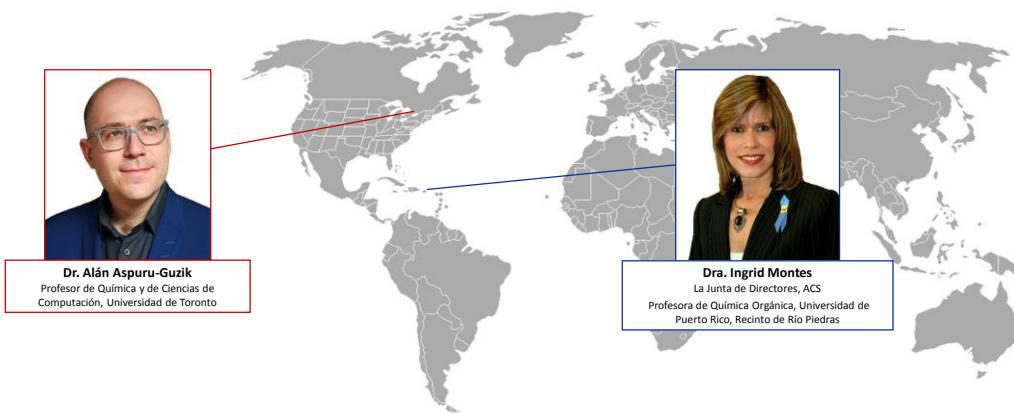
Alberto Nuñez Sellés,  
*Universidad Nacional Evangélica*

<http://bit.ly/ACS-SQMwebinars>

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## “Cómputo Cuántico para Química”



**Dr. Alán Aspuru-Guzik**  
Profesor de Química y de Ciencias de Computación, Universidad de Toronto

**Dra. Ingrid Montes**  
La Junta de Directores, ACS  
Profesora de Química Orgánica, Universidad de Puerto Rico, Recinto de Río Piedras

*Las imágenes de la presentación están disponibles para descargar ahora desde el panel de GoToWebinar*

<http://bit.ly/ComputoCuantico>

El Webinar de hoy está auspiciado por la Sociedad Química de México y the American Chemical Society

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# The Age of Variational Quantum Algorithms

Alán Aspuru-Guzik

Professor of Chemistry  
Professor of Computer Science  
University of Toronto  
Vector Institute for Artificial Intelligence



VECTOR INSTITUTE | INSTITUT VECTEUR

Chief Scientific Officer  
Zapata Computing



Zapata Computing

Chief Vision Officer  
Kebotix

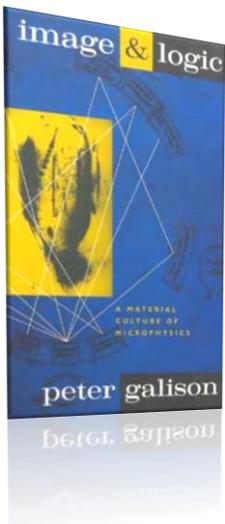


# Early classical mechanical simulators

Antikythera Mechanism  
circa 200 BC



# Digital Computer Simulation



Without the computer-based simulation, the material culture of late-twentieth-century microphysics is not merely inconvenienced – It does not exist. [...] Machines [...] are inseparable from their virtual counterparts – all are bound to simulations.

–Peter Galison

From *Image and Logic: A material culture of microphysics* (1997)

# Simulating Matter



Flow batteries

e.g. Huskinson, et al., Nature 505 195 2014

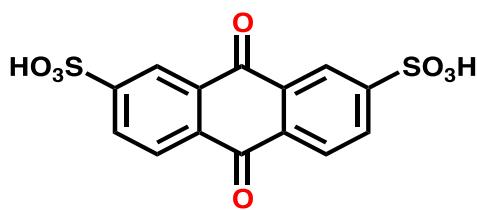


Organic light-emitting diode displays

e.g. R. Gomez-Bombarelli, Nature Materials 15, 1120 2016

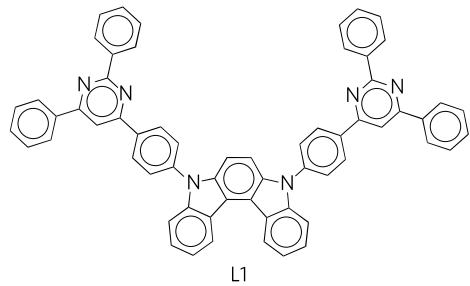
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# Simulating Matter



Flow batteries

e.g. Huskinson, et al., Nature 505 195 2014

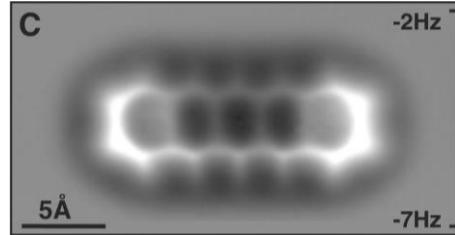


# Simulating Matter



Flow batteries

e.g. Huskinson, et al., Nature 505 195 2014

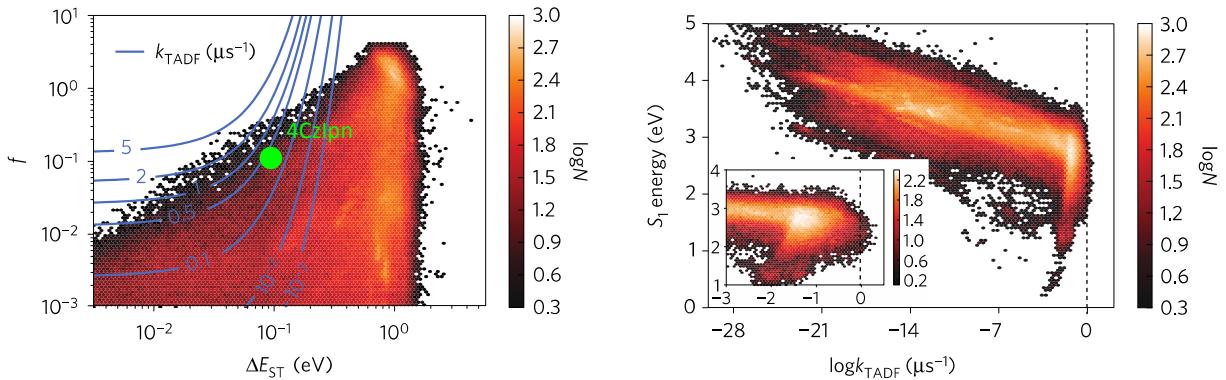


Pentacene on a surface

Gross et. al., Science 325 1110 2009

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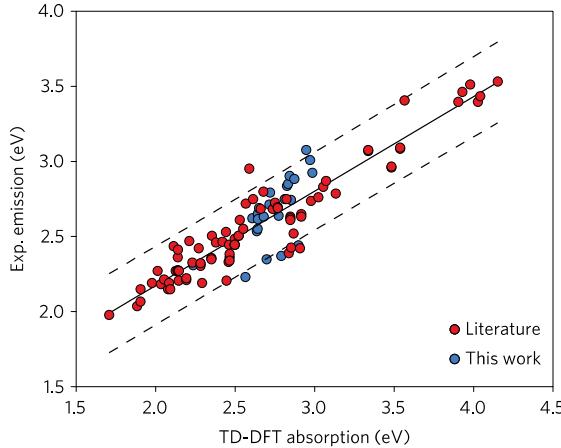
## Data Mining 500,000 Quantum Calculations



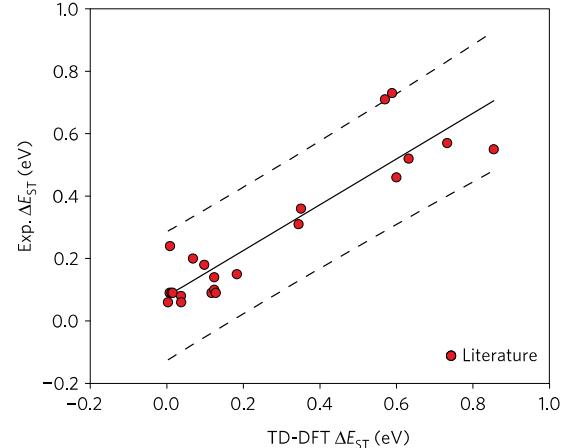
R. Gomez-Bombarelli, et al. Nature Materials 15, 1120 2016

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# Calibration of TDDFT with Experiment

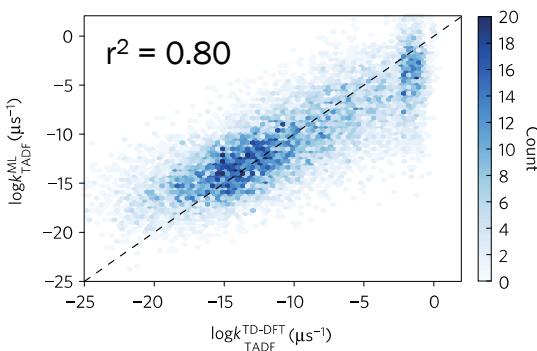


TD-DFT/B3LYP/6-31G(d) vertical absorption against PL emission maximum in **toluene**

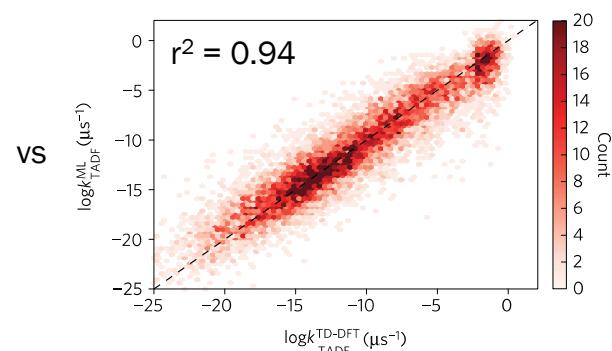


TD-DFT/B3LYP/6-31G(d) ST-Gap vs thermal activation in frozen **toluene**

# Machine Learning



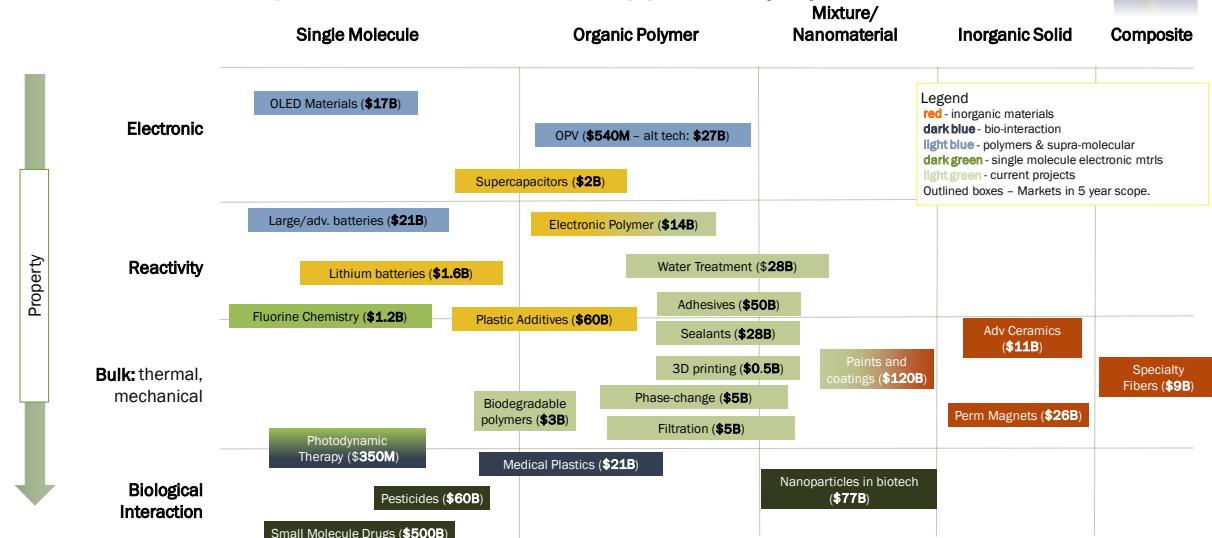
Linear regression model (c.f. QSAR)



Convolutional neural network  
(modern machine learning)



## Estimated Capabilities and Market Opportunity by 2025

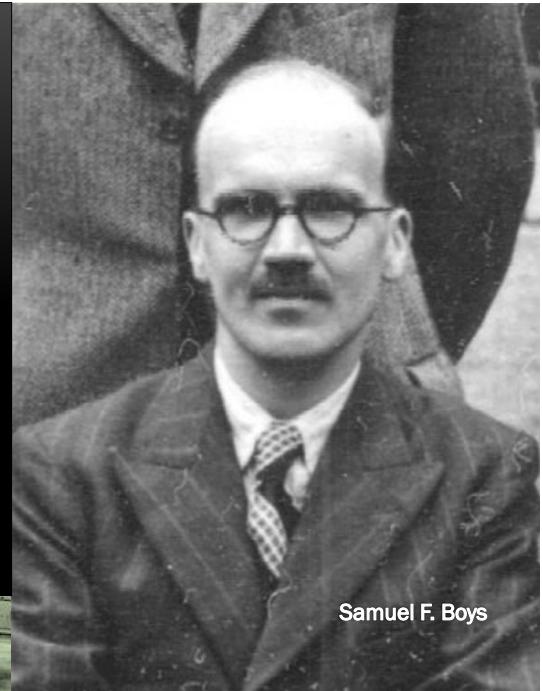


\*market info source: BCC Research Inc, multiple research reports (2012-2015) 21

“[H]e produced a paper tape of his whole computer program and unrolled it along the length of the chemical lecture bench. There, in one roll, was something, of which one could ask a chemical question at one end and it would produce an answer at the other! . . . most of the audience probably thought the demonstration bizarre. But it was prescient”



Handy, Pople, Shavitt, JPCA (1996)



Samuel F. Boys

# Classical Computer Algorithms

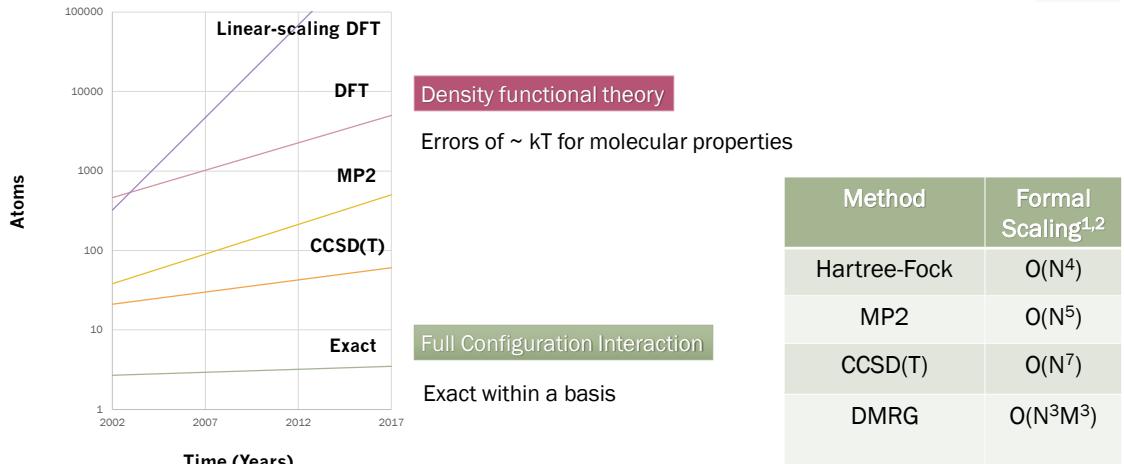
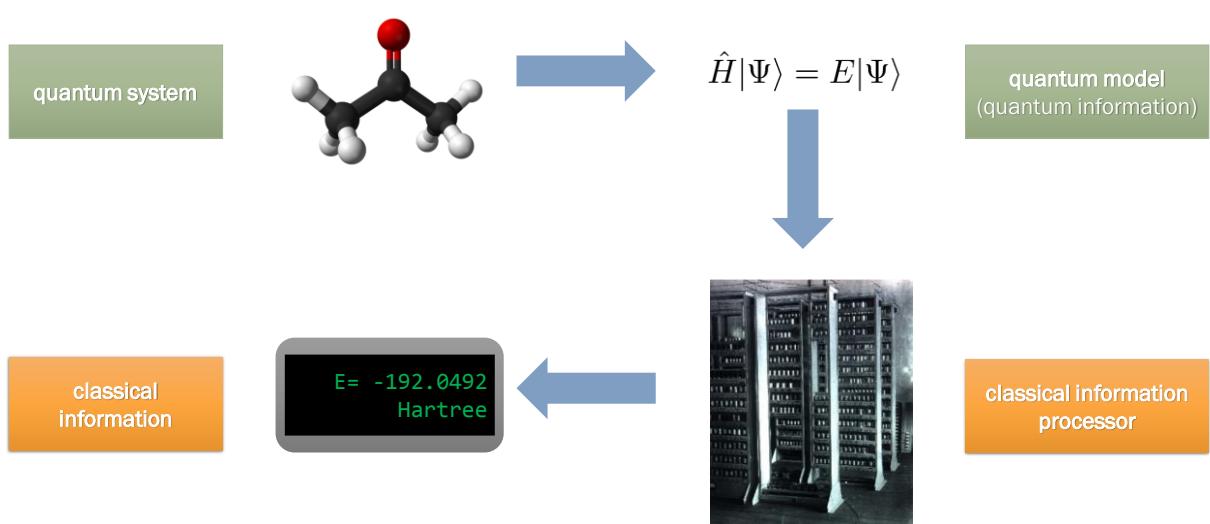


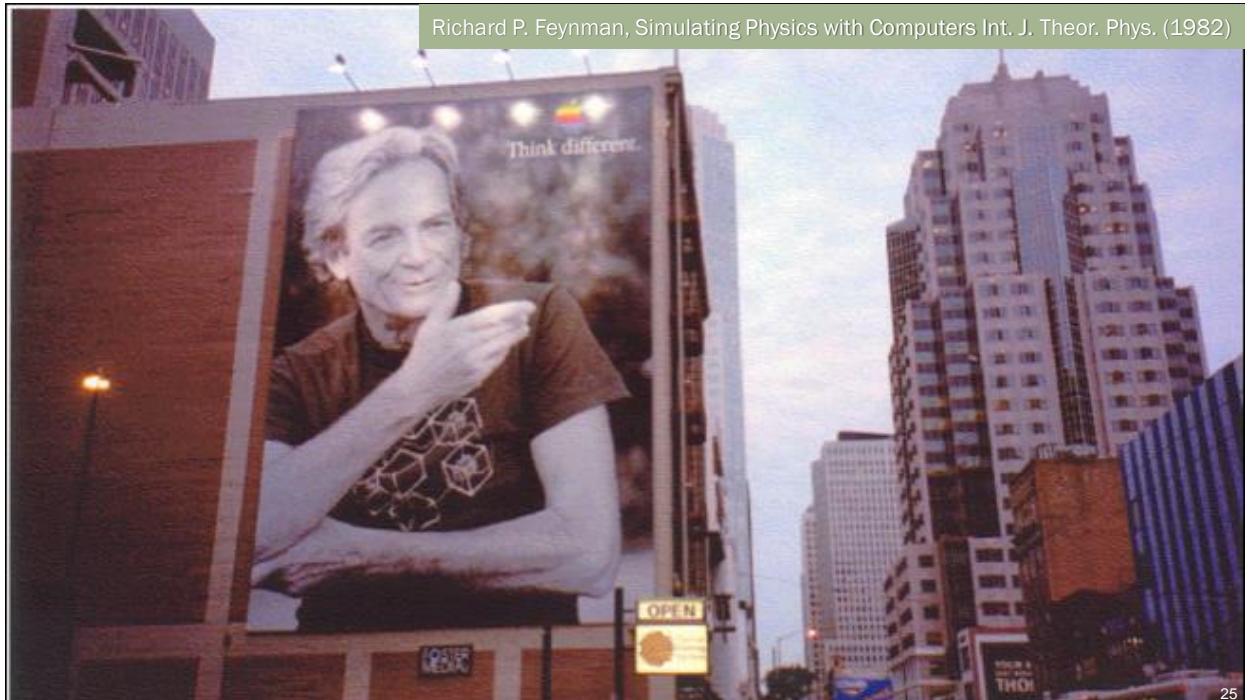
Figure adapted from M. Head-Gordon, M. Artacho, *Physics Today* 4 (2008)

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## The Current Paradigm



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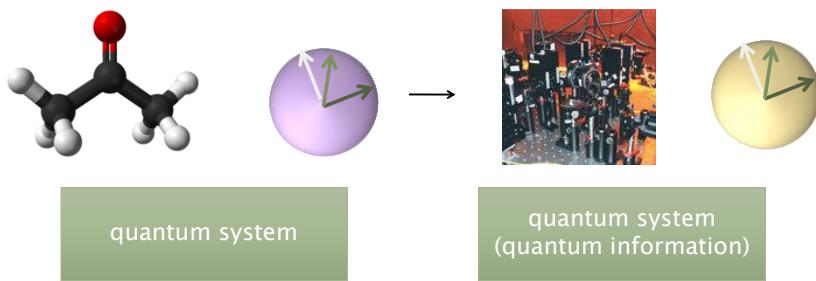


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## Quantum Computer Simulation

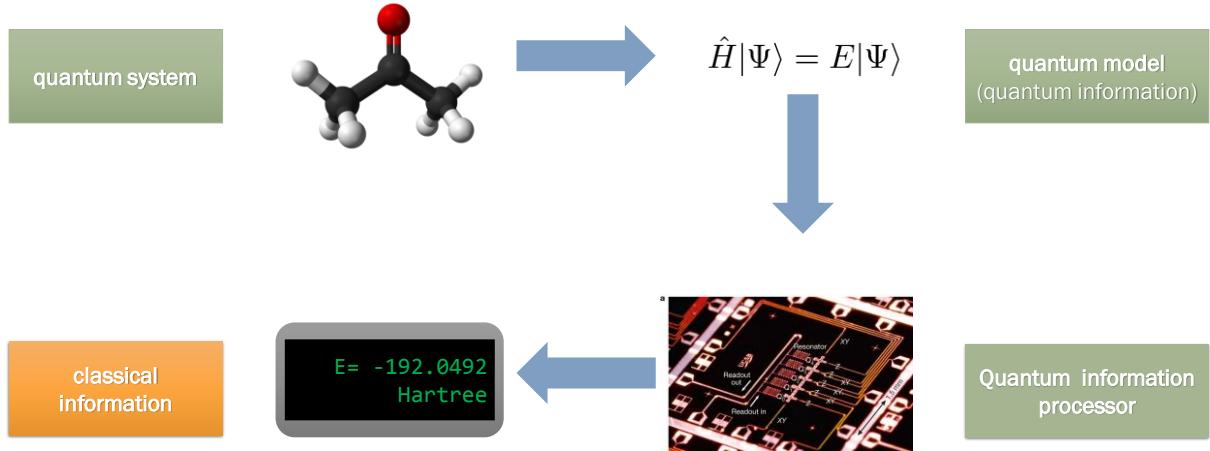


$$\begin{aligned} |\Psi^{mol}\rangle &\rightarrow |\Psi^{QC}\rangle \\ \hat{U}^{mol}(t) = e^{-i\hat{H}^{mol}t} &\rightarrow \hat{U}^{QC}(t) = e^{-i\hat{H}^{QC}t} \end{aligned}$$



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# The Quantum Simulation Way



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# Disruption and Quantum Supremacy

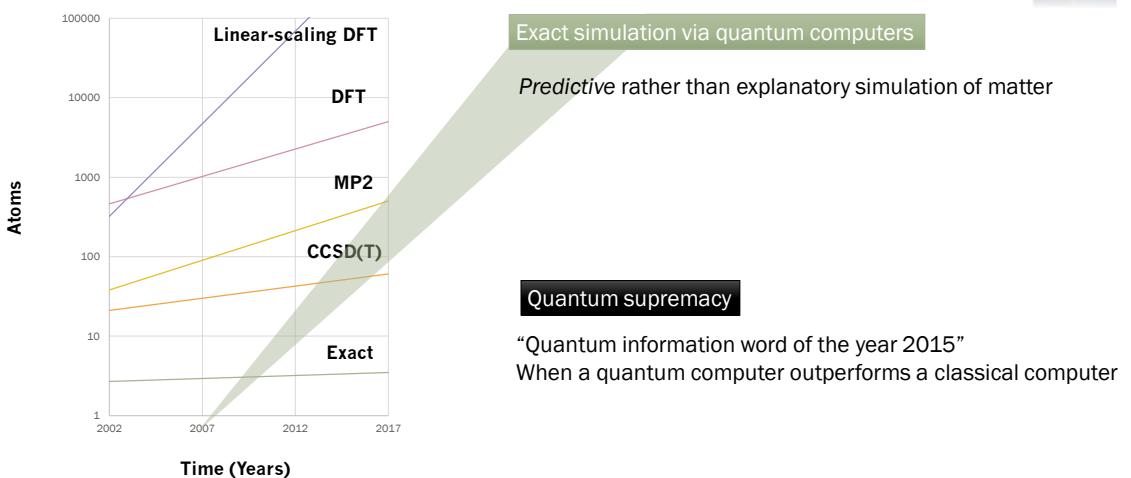
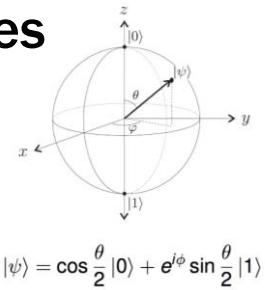
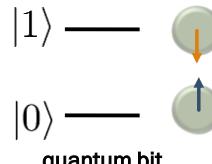
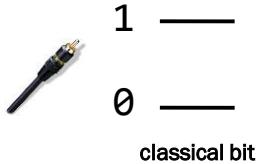


Figure adapted from M. Head-Gordon, M. Artacho, *Physics Today* 4 (2008)

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# Quantum Computers in 3 slides



Bloch sphere

quantum bit

Superposition

Entanglement

Collapse upon measurement

quantum computer

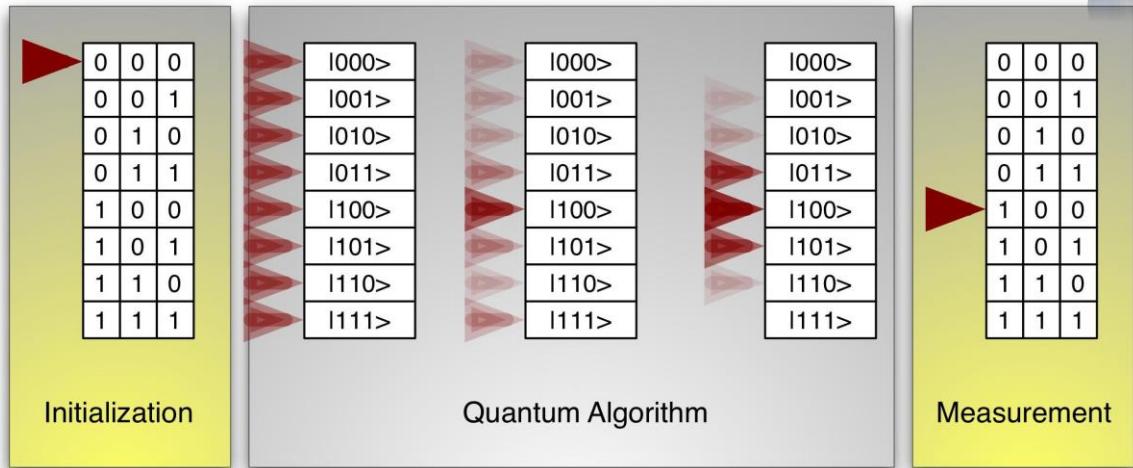
Collection of controllable qubits

Subject to decoherence

Ability for quantum error correction

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# Quantum Computation



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# Quantum Gates and Circuits



## Single qubit gates

Rotations

$$\begin{aligned} \text{---} \boxed{R_{\hat{n}}} \text{---} &= \exp[-i(\vec{\sigma} \cdot \hat{n})\theta/2] \\ \vec{\sigma} &\equiv [\sigma_x, \sigma_y, \sigma_z] \end{aligned}$$

Hadamard gate

$$\text{---} \boxed{H} \text{---} = \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$



## Two qubit gates

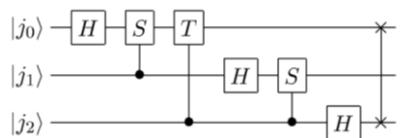
Controlled-not (CNOT) gate

$$\text{---} \boxed{\text{CNOT}} \text{---} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

$$\begin{aligned} |00\rangle &\rightarrow |00\rangle \\ |01\rangle &\rightarrow |01\rangle \\ |10\rangle &\rightarrow |11\rangle \\ |11\rangle &\rightarrow |10\rangle \end{aligned}$$

## Subroutines

Quantum Fourier Transform



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# The Power of Quantum Computers



## Myth

Quantum algorithms are always faster and more efficient than classical ones

## Quantum algorithm hall of fame

Search

quadratic speedup

Factoring

exponential speedup

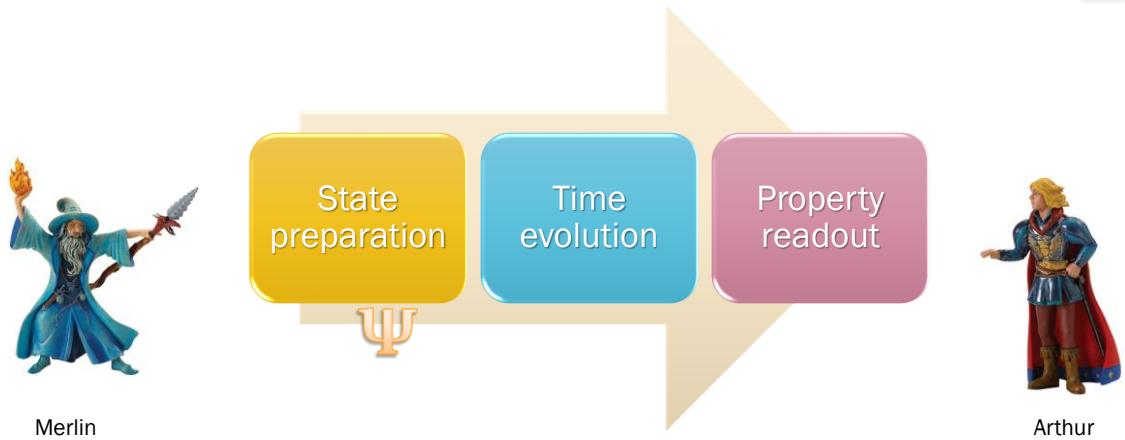
Quantum simulation

exponential speedup\*

\* Restrictions may apply. Read your owner's manual.

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# Quantum Computer Simulation



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## Complexity Classes



- Quantum Merlin Arthur  
(**Complete**: two-body Hamiltonian problem)

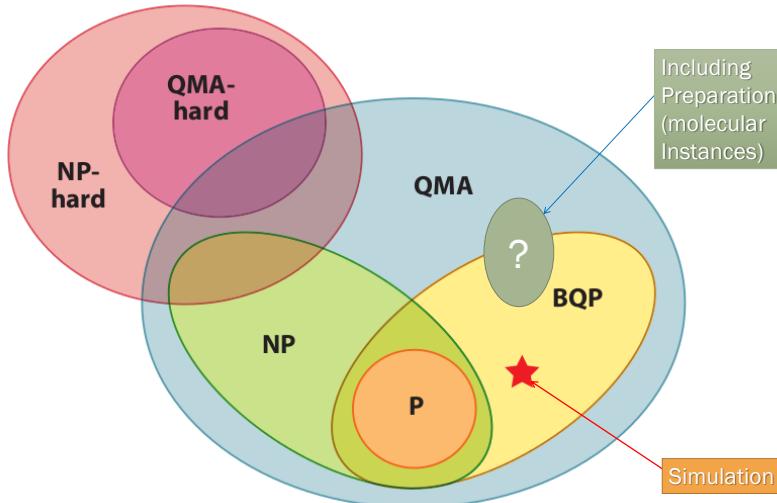
Decision problems that have a proof that can be verified by a quantum computer

- Bounded Quantum Polynomial (BQP)

The class of decision problems **solvable in polynomial time** by a quantum computer

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# Quantum Complexity of Chemical Simulation



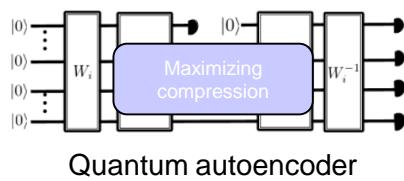
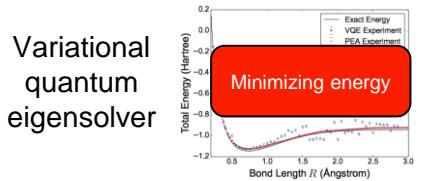
<http://www.youtube.com/watch?v=6ybd5rbQ5rU>

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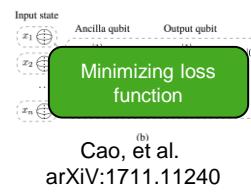
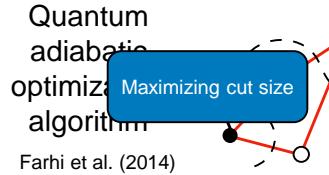


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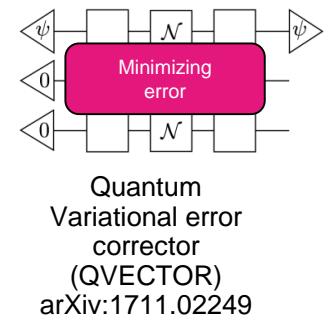
## The age of variational quantum algorithms ... training quantum circuits.



Romero, et al.  
Quantum Sci. Technol. 2 (2017): 045001



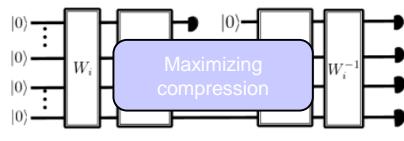
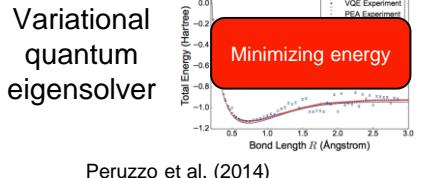
Quantum neuron



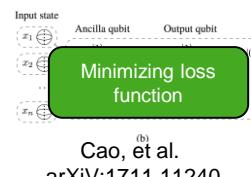
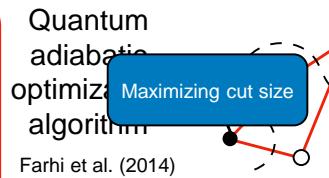
... and many other algorithms, e.g. Machine Learning

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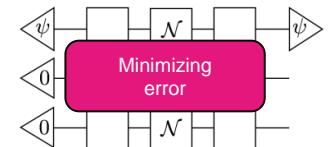
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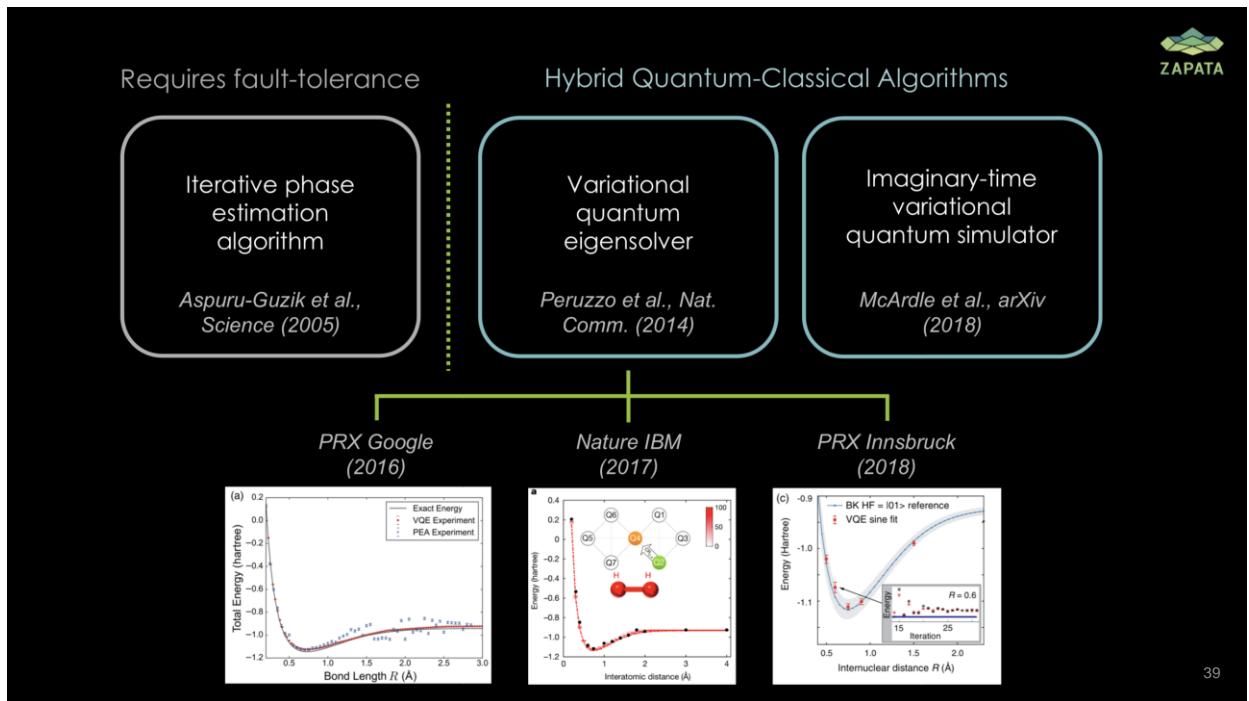


Quantum neuron



... and many other algorithms, e.g. Machine Learning

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## The Variational Quantum Eigensolver (VQE)



Peruzzo, McClean, Shadbolt, Yung, Zhou, Love, Aspuru-Guzik, O'Brien. *Nature Communications* 5 4213 2014

Romero, et al arXiv:1701.02691. *Quantum Science and Technology* (2018) In Press

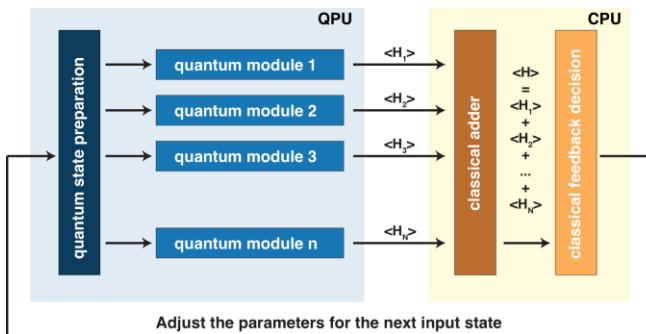
# The Variational Quantum Eigensolver (VQE)



Minimize energy:  $\underset{|\psi\rangle}{\operatorname{argmin}} \frac{\langle\psi| \mathcal{H} |\psi\rangle}{\langle\psi|\psi\rangle}$ .

$$\mathcal{H} = h_{\alpha}^i \sigma_{\alpha}^i + h_{\alpha\beta}^{ij} \sigma_{\alpha}^i \sigma_{\beta}^j + h_{\alpha\beta\gamma}^{ijk} \sigma_{\alpha}^i \sigma_{\beta}^j \sigma_{\gamma}^k + \dots$$

$$\langle\psi| \mathcal{H} |\psi\rangle \equiv \langle\mathcal{H}\rangle = \mathcal{H} = h_{\alpha}^i \langle\sigma_{\alpha}^i\rangle + h_{\alpha\beta}^{ij} \langle\sigma_{\alpha}^i \sigma_{\beta}^j\rangle + h_{\alpha\beta\gamma}^{ijk} \langle\sigma_{\alpha}^i \sigma_{\beta}^j \sigma_{\gamma}^k\rangle + \dots$$



Peruzzo, McClean, Shadbolt, Yung, Zhou, Love, Aspuru-Guzik, O'Brien. Nature Communications 5 4213 2014

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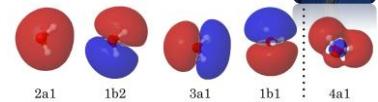
## Quantum Chemistry in 1 Slide



Self-consistent solution in local basis



Molecular orbitals and “integrals”



### Molecular Hamiltonian

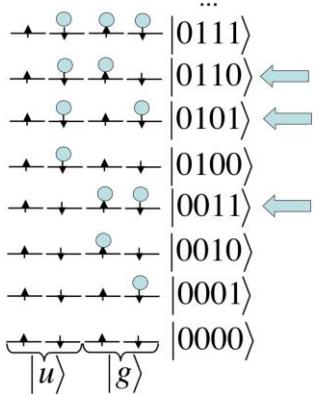
$$\hat{H} = \sum_X \hat{h}_X = \sum_{p,q} \langle p | \hat{T} + \hat{V}_N | q \rangle \hat{a}_p^\dagger \hat{a}_q \pm \frac{1}{2} \sum_{p,q,r,s} \langle p | \langle q | \hat{V}_e | r \rangle | s \rangle \hat{a}_p^\dagger \hat{a}_q^\dagger \hat{a}_r \hat{a}_s$$

One electron integrals

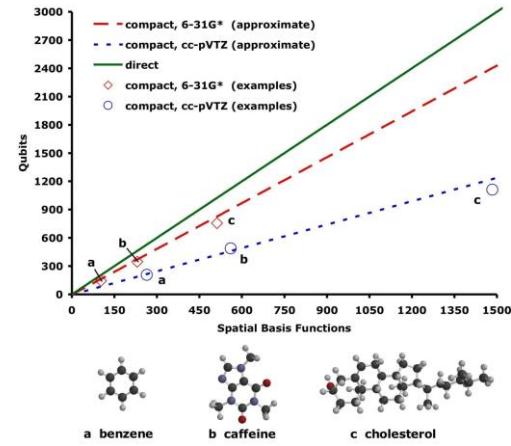
Two-electron integrals

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# Mapping and Baseline Resource Requirements



Direct mapping



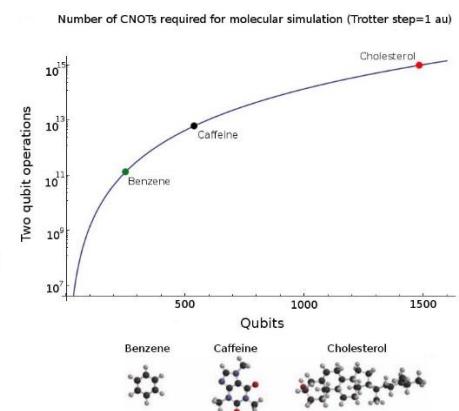
A. Aspuru-Guzik, A. D. Dutoi, P. J. Love, M. Head-Gordon, Science (2005) **Full quantum circuit:** J. D. Whitfield, et. al., Mol. Phys. (2011) **Error correction:** N. Cody Jones, J. D. Whitfield, et al. New. J. Phys.(2012)

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## Steep Scaling for Baseline Algorithm



$$\begin{aligned}
 & h_{pp} a_p^\dagger a_p & - \boxed{T(\theta)} - \\
 & h_{pq} a_p^\dagger a_q + h_{qp} a_q^\dagger a_p & \\
 & h_{ppqr} a_p^\dagger a_q^\dagger a_r a_p + h_{rqpp} a_p^\dagger a_q^\dagger a_q a_p & \\
 & h_{pqrs} a_p^\dagger a_q^\dagger a_r a_s + h_{srqp} a_s^\dagger a_q^\dagger a_q a_p & \text{where } M = H \text{ and } Y \\
 & & p - [M] \cdots [M] - \\
 & & q+1 \quad \oplus \quad \cdots \quad \oplus \quad q \\
 & & q-1 \quad \oplus \quad \cdots \quad \oplus \quad r \\
 & & r - [M] \cdots [R_z] \cdots [M] \\
 & & \text{where } (M_1, M_2, M_3, M_4) = \\
 & & (H, H, H, H), (H, Y, H, Y), (Y, H, Y, H), \\
 & & (Y, Y, H, H), (H, H, Y, Y), (Y, H, Y, Y), \\
 & & (H, Y, Y, H) \text{ and } (Y, Y, Y, Y) \\
 & & p - [M_1] \cdots [M_1] - \\
 & & q - [M_2] \cdots [M_2] - \\
 & & r - [M_3] \cdots [M_3] - \\
 & & s - [M_4] \cdots [R_z(\theta)] \cdots [M_4] - \\
 \text{Notation:} & \begin{array}{c} \bullet \\ \oplus \end{array} = \begin{array}{c} \bullet \\ \oplus \\ \bullet \\ \oplus \end{array}
 \end{aligned}$$



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# Experimental Implementations



## Quantum optics

Hydrogen molecule HeH <sup>+</sup>	2 qubits 2 qubits	Lanyon, et al., Peruzzo, et al.,	Nat Chem 2 106 Nat Comms 5 4213	2010 2014
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## Nuclear Magnetic Resonance

Hydrogen molecule	2 qubits	Du, et al,	Phys Rev Lett 104 030502	2010
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## Nitrogen vacancy centers

HeH <sup>+</sup>	2 qubits	Wang, et al.,	ACS Nano 9 7769	2015
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## Superconducting qubits

Hydrogen molecule BeH <sub>2</sub>	3 qubits 6 qubits	O'Malley, et al, Kandala, et al.	Phys Rev X 6 031007 Nature 548 242	2016 2017
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## Ion traps

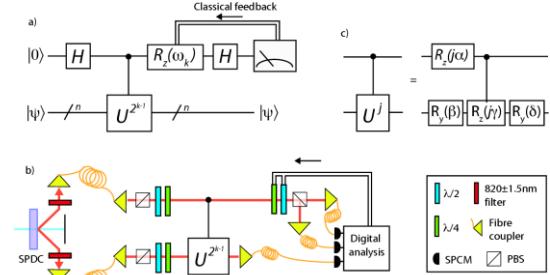
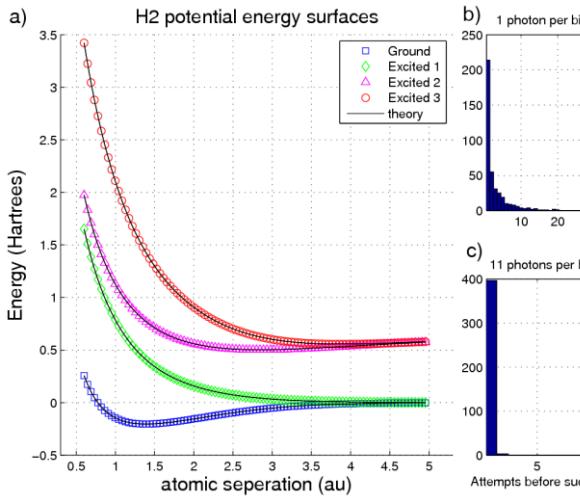
HeH+ LiH	3 qubits 3 qubits	Shen, et al, Hempel, et al.	arXiv:1506.00443 To be submitted	2015 2016
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45



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# First Quantum Simulation of Hydrogen Molecule Potential Energy Surface



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## Hierarchy of Post-HF Methods



We can recover the **electron correlation** by expanding the wavefunction in the configurational space.

$$\begin{array}{cccc}
 |\Phi_0\rangle & |\Phi_i^a\rangle & |\Phi_{ij}^{ab}\rangle & \Phi_i^a = a_a^\dagger a_i |\Phi_0\rangle \\
 \boxed{\begin{array}{c} \uparrow \\ \uparrow \\ \downarrow \\ \uparrow \\ \downarrow \\ \uparrow \\ \downarrow \end{array}} + \dots + \boxed{\begin{array}{c} \uparrow \\ \uparrow \\ \uparrow \\ \uparrow \\ \uparrow \\ \uparrow \\ \downarrow \end{array}} + \dots + \boxed{\begin{array}{c} \uparrow \\ \uparrow \\ \downarrow \\ \uparrow \\ \downarrow \\ \uparrow \\ \downarrow \end{array}} + \dots & \Phi_{ij}^{ab} = a_a^\dagger a_b^\dagger a_i a_j |\Phi_0\rangle & \binom{N}{\eta} \text{ determinants} \\
 |FCI\rangle = \left( c_0 + \sum_{i,a} c_i^a a_a^\dagger a_i + \sum_{i>j, a>b} c_{ij}^{ab} a_a^\dagger a_i a_j + \dots \right) |\Phi_0\rangle & \text{Configuration interaction (CI)} \\
 |CC\rangle = \exp \left( \sum_{i,a} t_i^a a_a^\dagger a_i + \sum_{i>j, a>b} t_{ij}^{ab} a_a^\dagger a_b^\dagger a_i a_j + \dots \right) |\Phi_0\rangle & \text{Coupled cluster (CC)}
 \end{array}$$

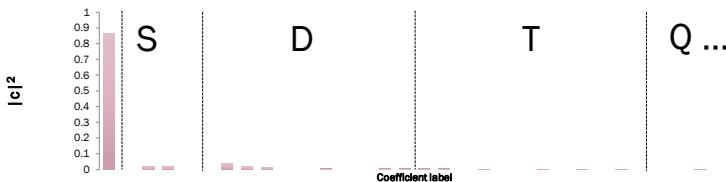
Helgaker, T., Jorgensen, P. and Olsen, J., 2014. Molecular electronic-structure theory.

48



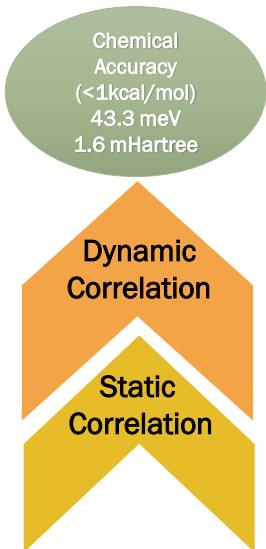
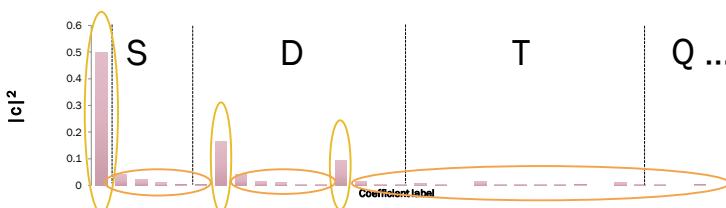
# Dynamic and Static Correlation

Single reference



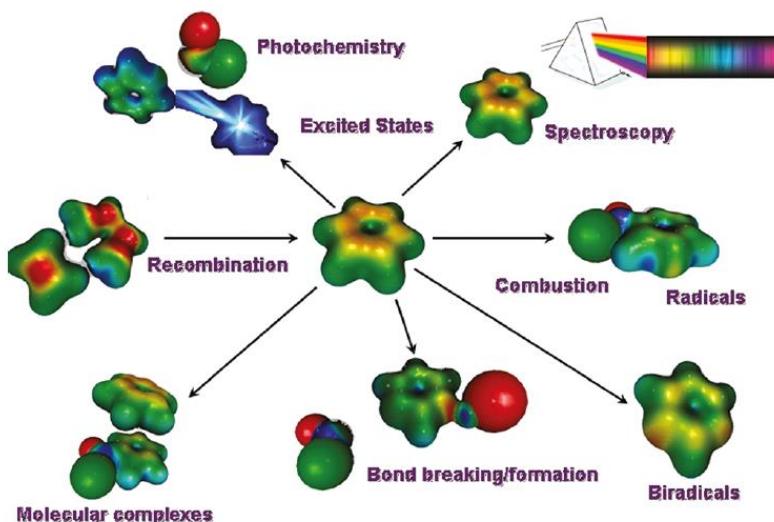
Chemical Accuracy  
( $<1\text{kcal/mol}$ )  
43.3 meV  
1.6 mHartree

Strongly correlated = “Multireference”



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## “Multireference” World of Chemistry

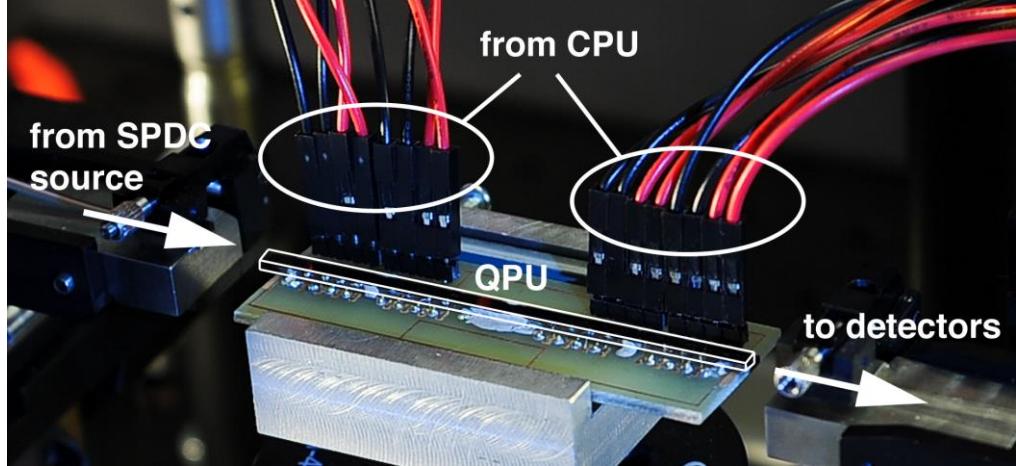


The accurate modeling of multireference phenomena is perhaps the biggest challenge for quantum chemistry.

From: Lyakh et al. *Chem. Rev.* **102**, 182, (2012).

50

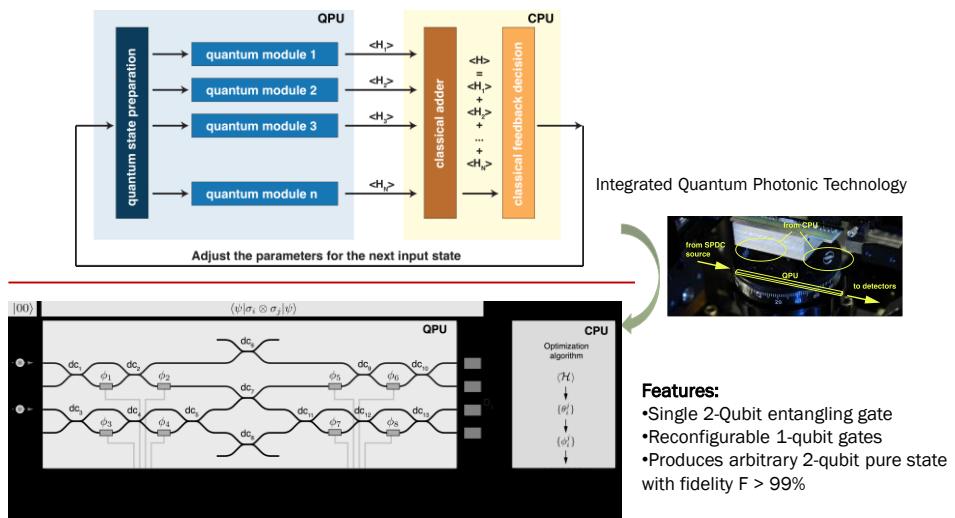
# The Variational Quantum Eigensolver (VQE)



Peruzzo, McClean, Shadbolt, Yung, Zhou, Love, Aspuru-Guzik, O'Brien. Nature Communications 5 4213 2014

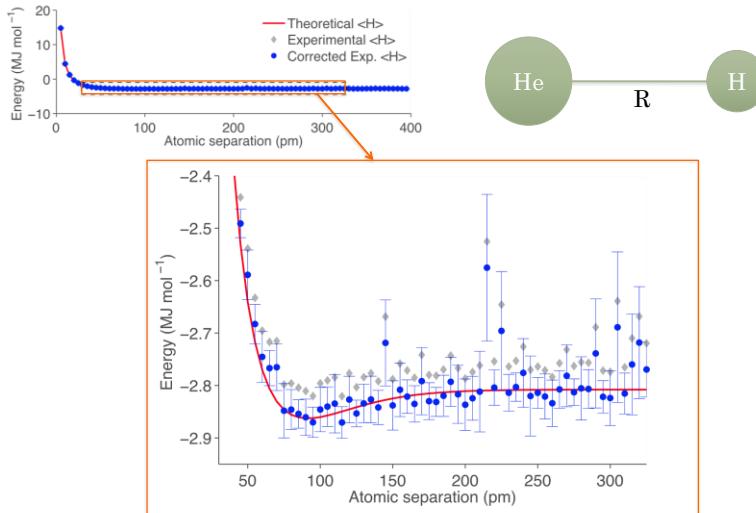
51

## Physical Implementation



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# Experimental Electronic Curve for HeH<sup>+</sup>



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# Unitary Coupled Cluster Ansatz



$$\begin{aligned} U(\vec{t}) &= \exp [-i(T - T^\dagger)] \\ &= \exp \left[ -i \sum_a t_a (\tau_a - \tau_a^\dagger) \right] \end{aligned}$$

$\tau_a$  : excitation operator

In a quantum computer we can implement an approximated unitary:

$$U(\vec{t}) \approx U_{Trot}(\vec{t}) = \left( \prod_i e^{\frac{t_i}{\rho} (\tau_i - \tau_i^\dagger)} \right)^\rho$$

Parameter scaling  
 $O(n_e^2 N^2)$

The BCH expansion for UCC is infinite.<sup>1</sup>

1. Taube, A.G. and Bartlett, R.J., 2006. Int. J. Quantum Chem. **106**(15), pp.3393-3401.

54

Romero, et al arXiv:1701.02691



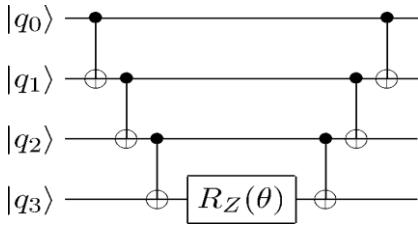
# VQE for UCC: How it all fits together

1 Second-quantized excitation operator

Jordan-Wigner transformation  
or Bravyi-Kitaev transformation

2 Pauli operators

3 Exponentiation



This circuit implements  $e^{-i\frac{\theta}{2}\sigma_3^Z\sigma_2^Z\sigma_1^Z\sigma_0^Z}$   
H and R<sub>x</sub> are used to change from Z to X and Y basis.

4 Measurement

|q<sub>3</sub>> — [Z] — [M]

|q<sub>2</sub>> — [Y] — [R<sub>x</sub>] — [M]

|q<sub>1</sub>> — [Z] — [M]

|q<sub>0</sub>> — [X] — [H] — [M]

... for all terms ...

Measuring the term  
 $\sigma_z^3\sigma_y^2\sigma_z^1\sigma_x^0$

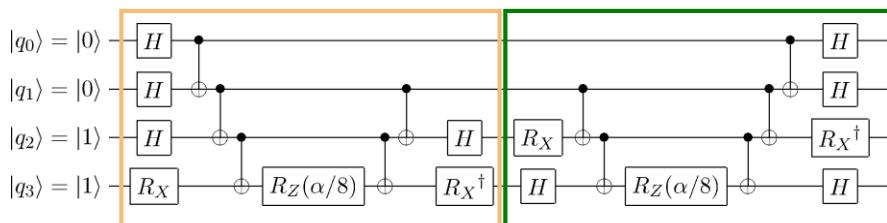
55

## Example: Minimal-basis H<sub>2</sub> Jordan-Wigner



$$\hat{H}_{JW} = f_1 \mathbf{1} + f_2(\sigma_0^z + \sigma_1^z) + f_3(\sigma_2^z + \sigma_3^z) + f_4\sigma_3^z\sigma_2^z + f_5\sigma_1^z\sigma_0^z + f_6(\sigma_2^z\sigma_0^z + \sigma_3^z\sigma_1^z) + f_7(\sigma_2^z\sigma_1^z + \sigma_3^z\sigma_0^z) + f_8(\sigma_3^x\sigma_2^y\sigma_1^z - \sigma_3^x\sigma_2^x\sigma_1^y\sigma_0^z + \sigma_3^y\sigma_2^x\sigma_1^x\sigma_0^y - \sigma_3^y\sigma_2^y\sigma_1^x\sigma_0^x)$$

$$\hat{U}(\alpha) = \exp[i\alpha/8(-\sigma_3^y\sigma_2^x\sigma_1^x\sigma_0^x - \sigma_3^x\sigma_2^y\sigma_1^x\sigma_0^x + \sigma_3^x\sigma_2^x\sigma_1^y\sigma_0^x + \sigma_3^x\sigma_2^x\sigma_1^x\sigma_0^y + \sigma_3^x\sigma_2^y\sigma_1^y\sigma_0^x + \sigma_3^y\sigma_2^x\sigma_1^y\sigma_0^x - \sigma_3^y\sigma_2^y\sigma_1^x\sigma_0^y - \sigma_3^y\sigma_2^y\sigma_1^y\sigma_0^x)]$$



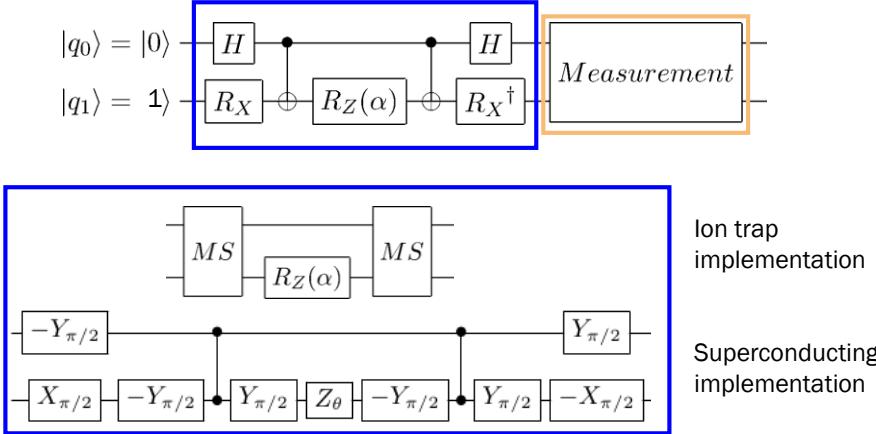
$$|0011\rangle \rightarrow (1-c)|0011\rangle + c|1100\rangle$$

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# Example: Minimal-basis H<sub>2</sub> Bravyi-Kitaev



$$H_2^{BK} = c_0 \mathbf{1} + c_1 \sigma_0^z + c_2 \sigma_1^z + c_3 \sigma_0^z \sigma_1^z + c_4 \sigma_0^x \sigma_1^x + c_5 \sigma_0^y \sigma_1^y$$



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Romero, et al arXiv:1701.02691

## Optimization of the Cost of UCC

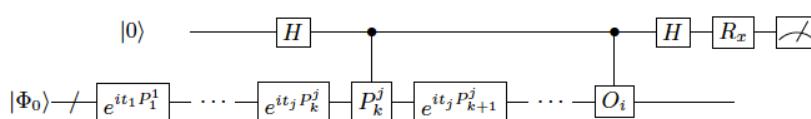
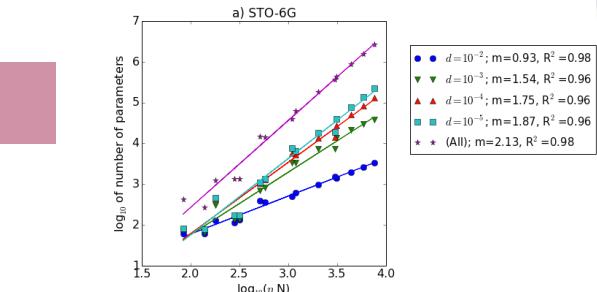


Use classical approximations of the amplitudes to reduce circuit size

Select terms using MP2

$$t_i^a = 0; \quad t_{ia}^{ab} = \frac{h_{ijba} - h_{ijab}}{\epsilon_i + \epsilon_j - \epsilon_a - \epsilon_b}$$

Gradients for UCC



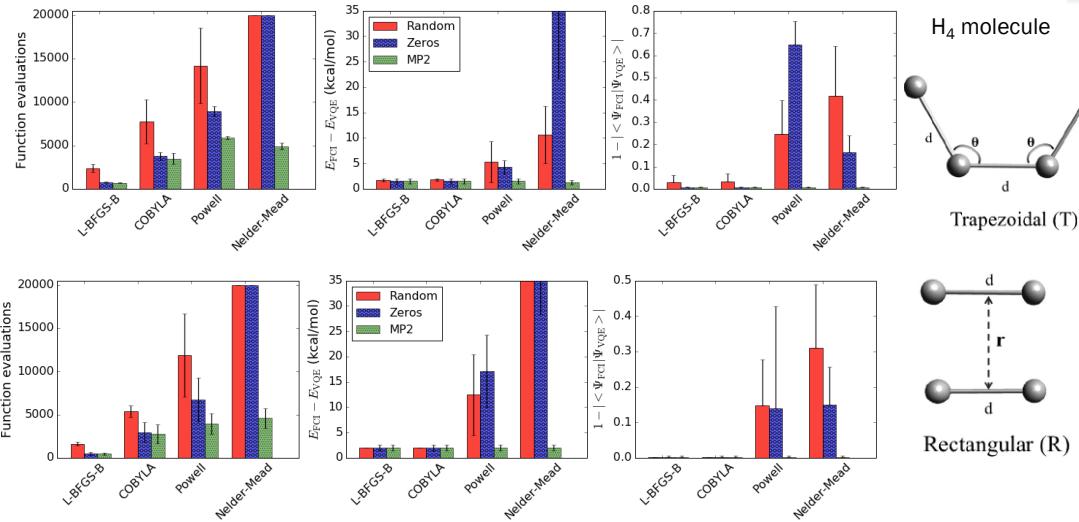
Romero et al. arXiv: 1701.02691 (2017).

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Romero, et al arXiv:1701.02691



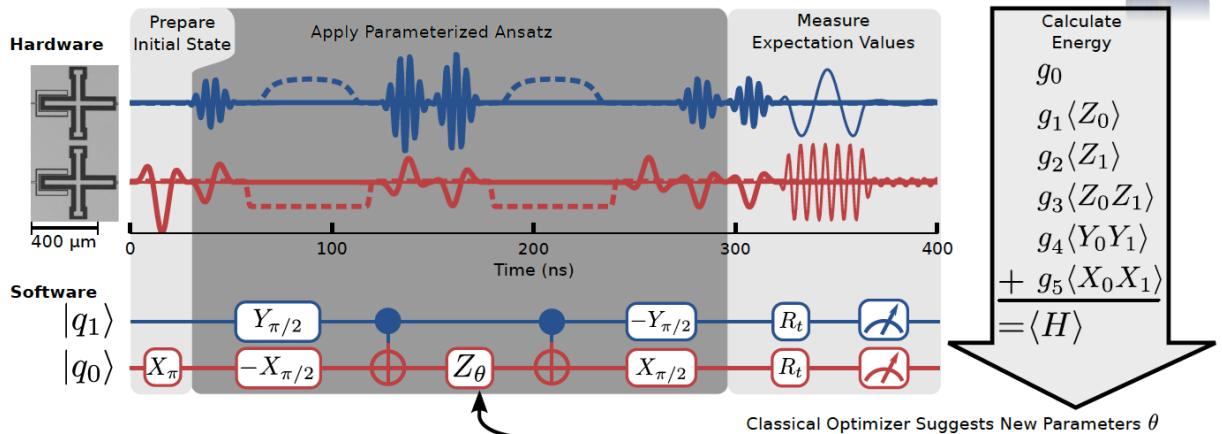
## Strategies for UCC Calculations



Romero et al. arXiv: 1701.02691 (2017).

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## Superconducting VQE for $H_2$

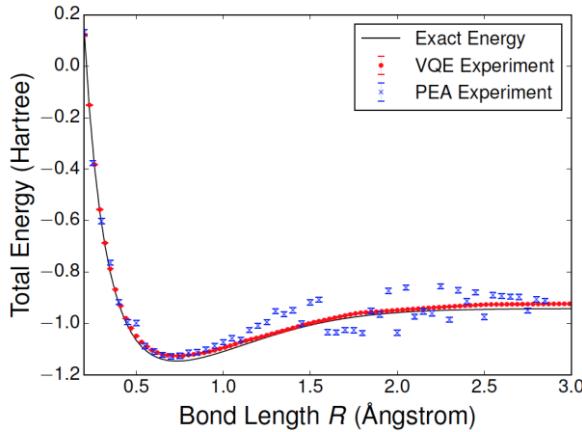


Used Xmon qubits to compute energy surface of molecular hydrogen  
Started in Hartree-Fock state, used unitary coupled cluster, got chemical accuracy

P. O'Malley, et al. Physical Review X 6 031007 2016

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# Superconducting VQE vs Phase Estimation



Predicted dissociation energy without exponentially costly compilation for first time  
Substantial robustness to systematic errors seen

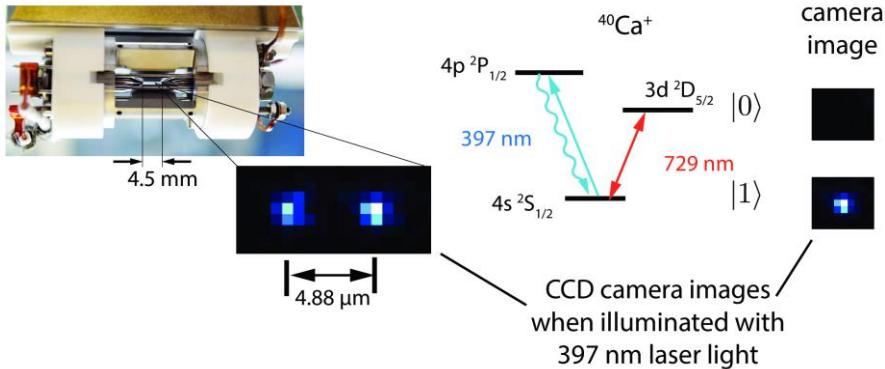
P. O'Malley, et al. Physical Review X 6 031007 2016

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## Ion Trap Implementation



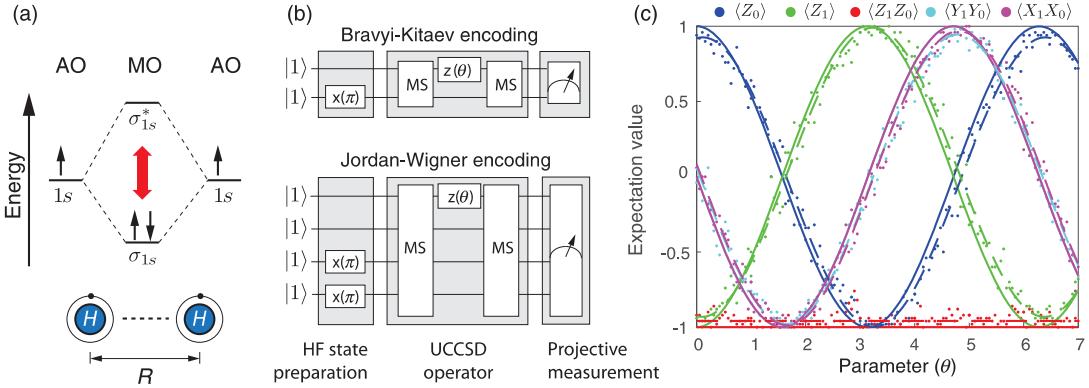
Collaboration with Rainer Blatt (Innsbruck)



Cornelius Hempel, Christine Maier, Jonathan Romero, Jarrod McClean, Thomas Monz, Heng Shen, Petar Jurcevic, Ben P. Lanyon, Peter Love, Ryan Babbush, Alán Aspuru-Guzik, Rainer Blatt, and Christian F. Roos  
Phys. Rev. X 8, 031022

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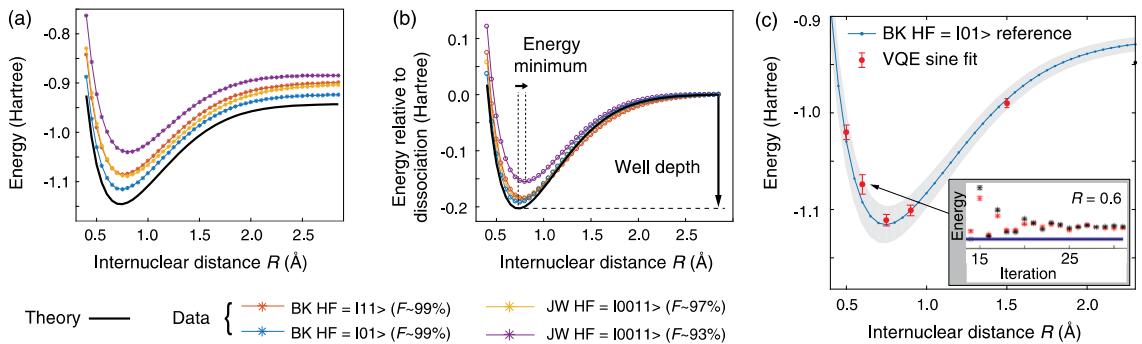
# Ion Trap Implementation ( $H_2$ )



Cornelius Hempel, Christine Maier, Jonathan Romero, Jarrod McClean, Thomas Monz, Heng Shen, Petar Jurcevic, Ben P. Lanyon, Peter Love, Ryan Babbush, Alán Aspuru-Guzik, Rainer Blatt, and Christian F. Roos  
 Phys. Rev. X **8**, 031022

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# Ion Trap Implementation ( $H_2$ )



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 Phys. Rev. X **8**, 031022

64

# Ion Trap Implementation ( $H_2$ )



Cornelius Hempel, Christine Maier, Jonathan Romero, Jarrod McClean, Thomas Monz, Heng Shen,  
Petar Jurcevic, Ben P. Lanyon, Peter Love, Ryan Babbush, Alán Aspuru-Guzik, Rainer Blatt, and Christian F. Roos  
Phys. Rev. X **8**, 031022

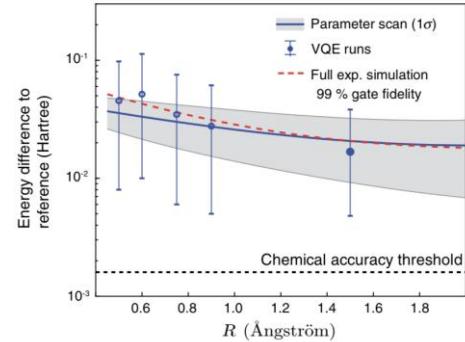
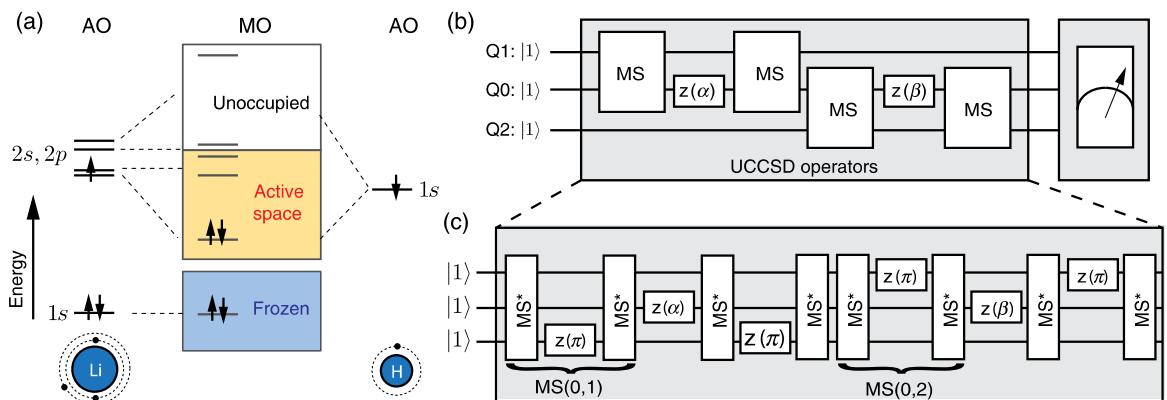


FIG. 7. Energy errors of the reconstructed  $H_2$  potential energy surface and the influence of decoherence. Differences are given with respect to the full configuration interaction (FCI) calculation performed in the chosen molecular basis. The red line corresponds to a full simulation of the quantum circuit, including multiple decoherence channels and the experimentally determined gate fidelity (see Appendix B 6 for details).

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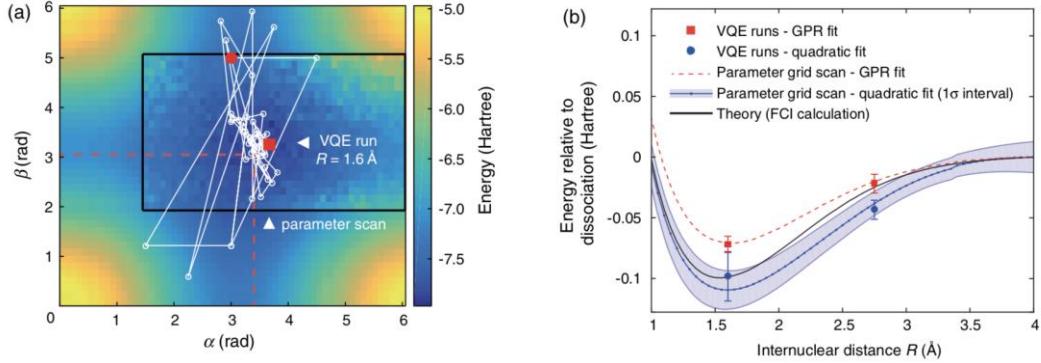
# Ion Trap Implementation ( $LiH$ )



Cornelius Hempel, Christine Maier, Jonathan Romero, Jarrod McClean, Thomas Monz, Heng Shen, Petar Jurcevic, Ben P. Lanyon, Peter Love, Ryan Babbush, Alán Aspuru-Guzik, Rainer Blatt, and Christian F. Roos  
Phys. Rev. X **8**, 031022

66

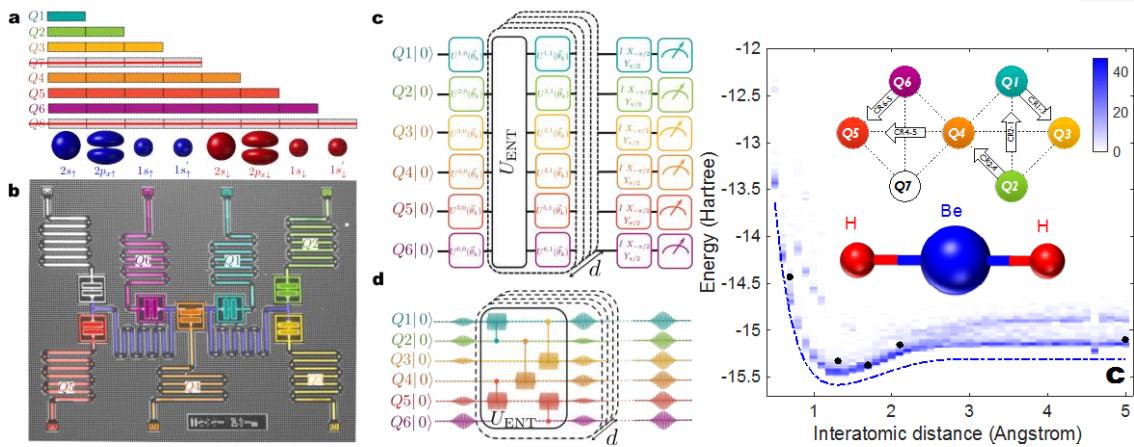
# Ion Trap Implementation (LiH)



Cornelius Hempel, Christine Maier, Jonathan Romero, Jarrod McClean, Thomas Monz, Heng Shen, Petar Jurcevic, Ben P. Lanyon, Peter Love, Ryan Babbush, Alán Aspuru-Guzik, Rainer Blatt, and Christian F. Roos  
Phys. Rev. X **8**, 031022

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# Variational Eigensolver by IBM Team!



Hardware-efficient Quantum Optimizer for Small Molecules and Quantum Magnets

Abhinav Kandala,\* Antonio Mezzacapo,\* Kristan Temme, Maika Takita, Jerry M. Chow, and Jay M. Gambetta  
IBM T.J. Watson Research Center, Yorktown Heights, NY 10598, USA  
(Dated: April 18, 2017)

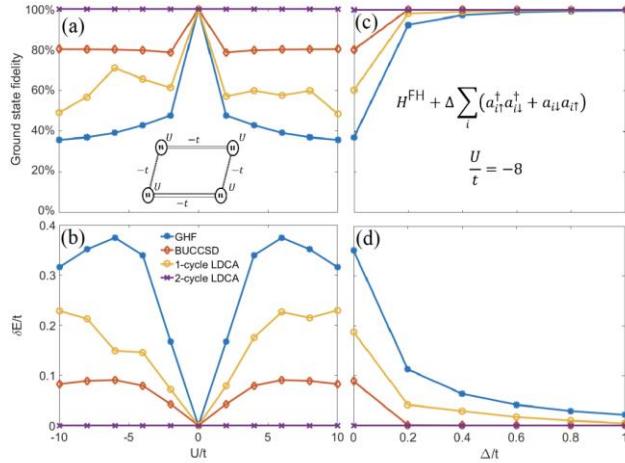
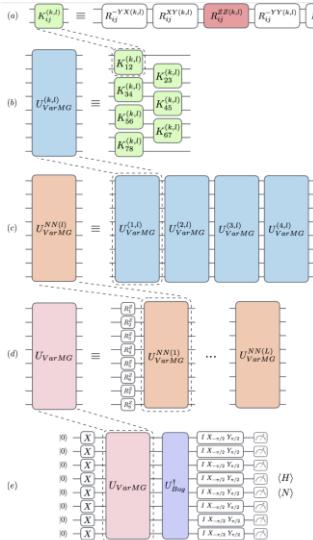
H-Be-H, 6 qubit simulations.

Kandala, et al Nature 549 242 (2017)

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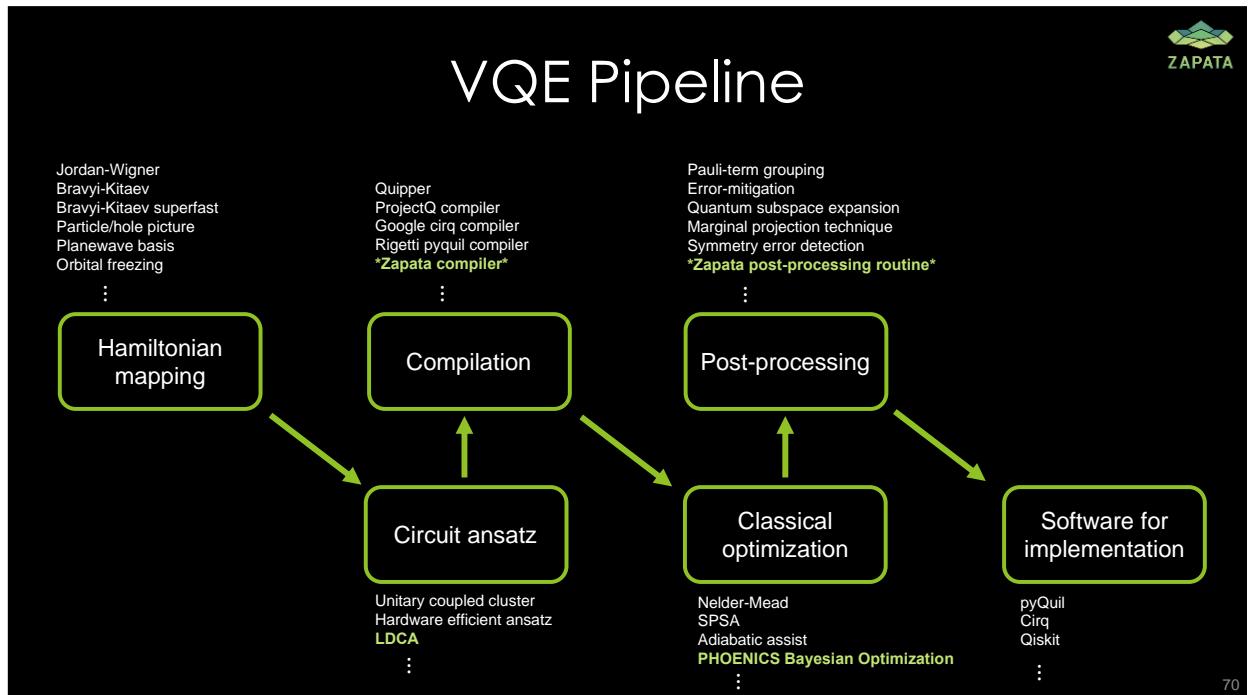
# Low-depth Correlated Ansatz (LDCA)

Approach motivated by Bogoliubov coupled cluster theory

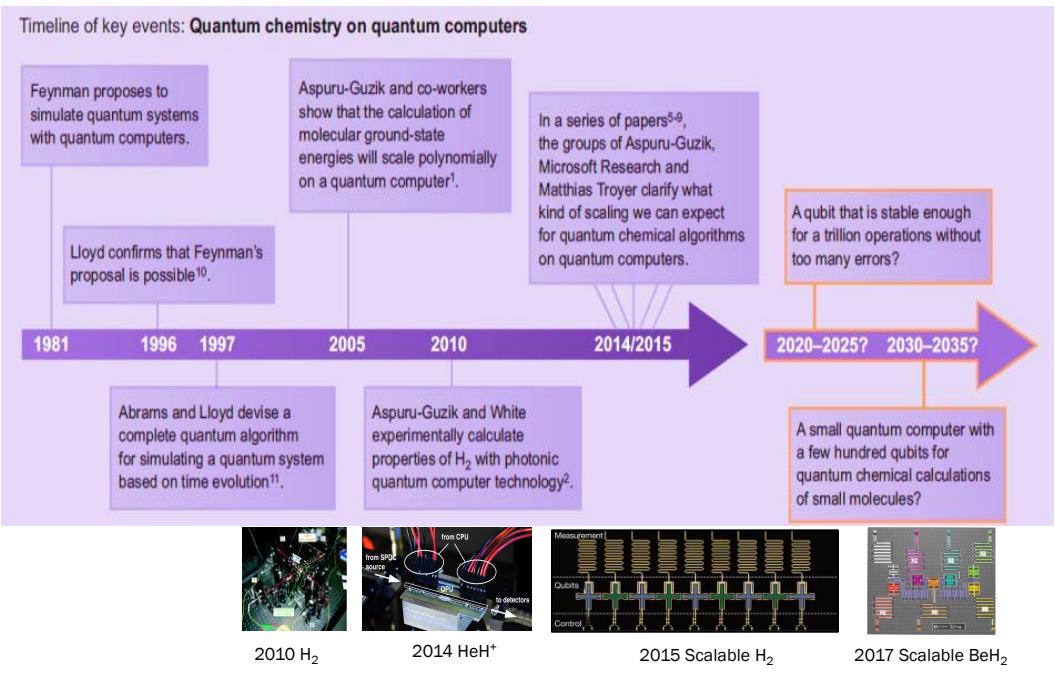


Dallaire-De Mers, J. Romero, L. Veis, S. Sim, A. Aspuru-Guzik arXiv:1801.01053 (2018)

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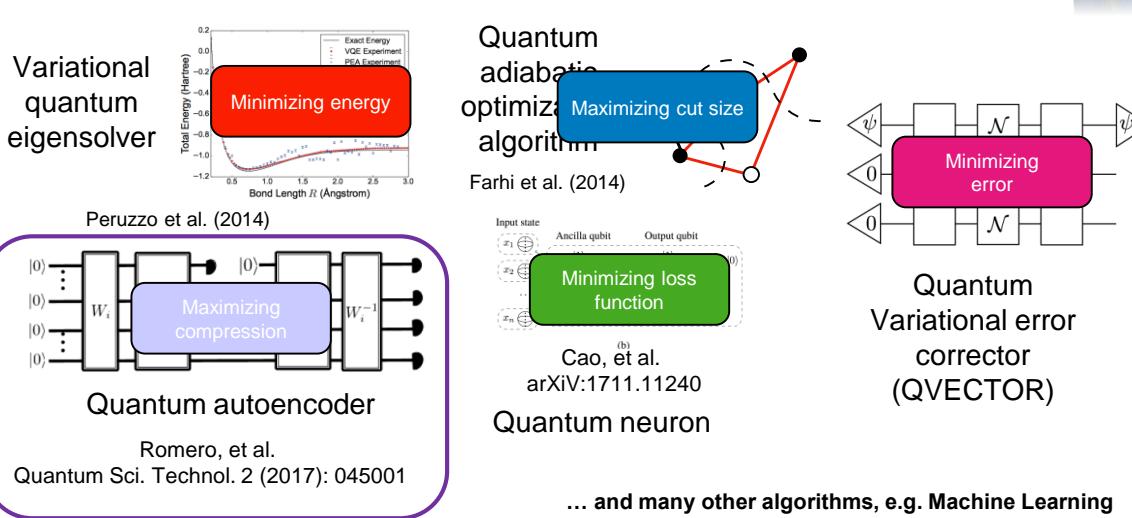
# Quantum Chemical Advantage?



Leonie Mueck. Nature Chemistry 7 361 2015

71

The age of variational quantum algorithms  
... training quantum circuits.



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# Machine Learning

The goal of *machine learning* is to design algorithms that can learn from and make predictions on data.



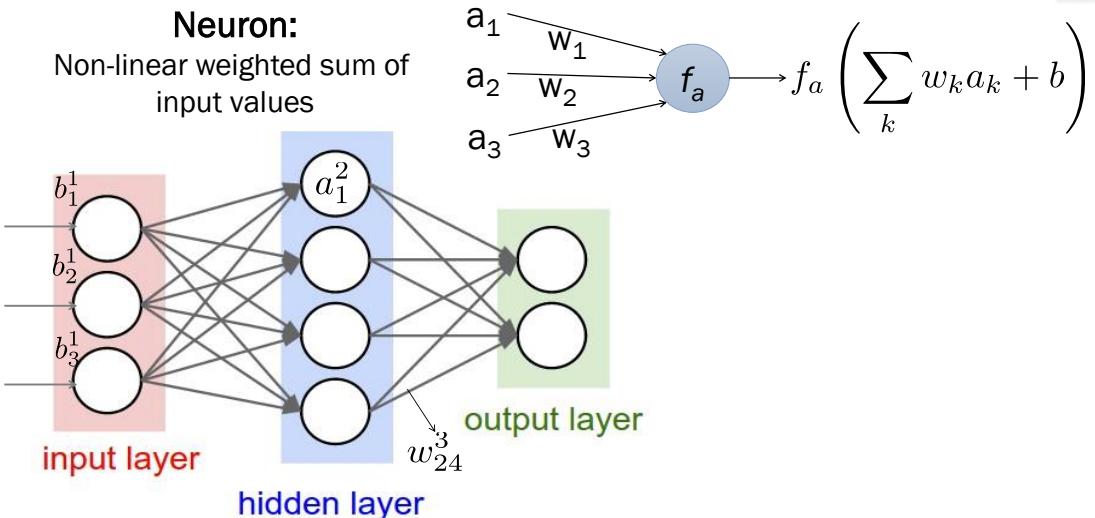
*“A computer program is said to learn from experience E with respect to a class of tasks T and performance measure P, if its performance at tasks T, as measured by P, improves with experience E”*

-Tom Mitchell (CMU)

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# Feedforward Neural Networks



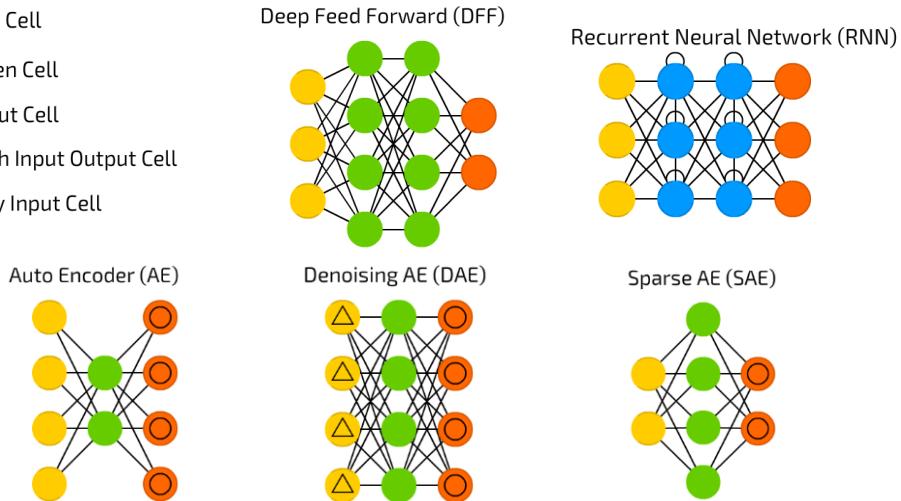
Michael A. Nielsen “Neural networks and deep learning”, Determination press. 2015.

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# Diversity of Neural Networks



- Input Cell
- Hidden Cell
- Output Cell
- Match Input Output Cell
- △ Noisy Input Cell



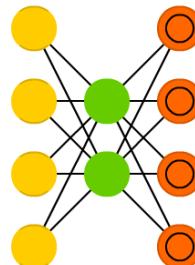
Reproduced from: <http://www.coolinfographics.com/blog/2016/9/20/the-mostly-complete-chart-of-neural-networks.html>. May 28 th, 2017.

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## Autoencoders



Image



Image



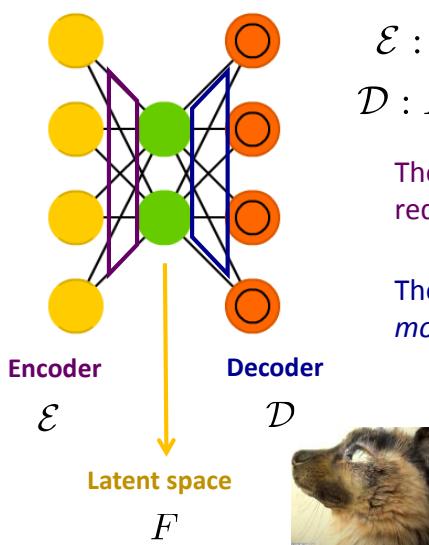
- Input Cell
- Hidden Cell
- Match Input Output Cell

Input      Hidden layers      Output

Image: asimovinstitute.org



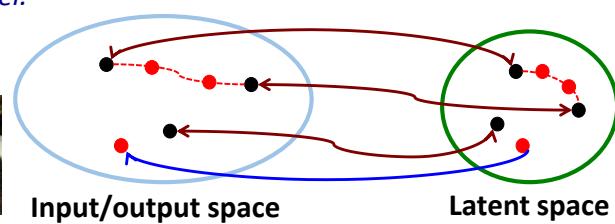
## Autoencoders



$$\begin{aligned} \mathcal{E} : X \rightarrow F & \quad \underset{\mathcal{E}, \mathcal{D}}{\operatorname{argmin}} \quad ||X - (\mathcal{D} \circ \mathcal{E})X||^2 \\ \mathcal{D} : F \rightarrow X' & \end{aligned}$$

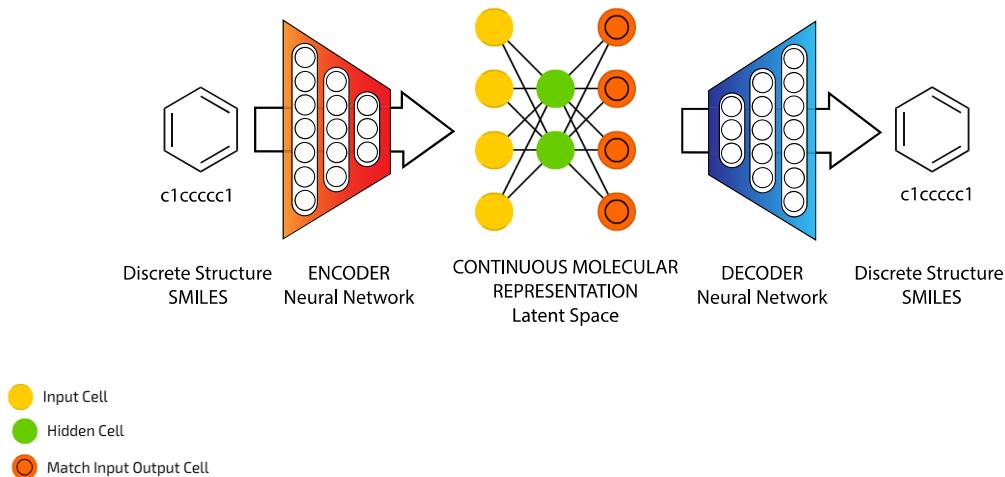
The encoding network can be used for dimensionality reduction and feature extraction

The decoding network can be used as a *generative model*.



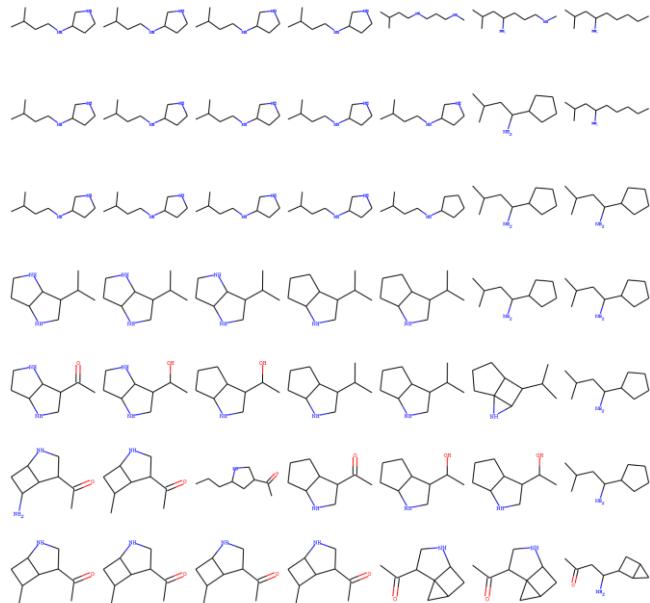
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# Autoencoders for Chemical Space



R. Gomez-Bombarelli, et al ACS Central Science 10.1021/acscentsci.7b00572 (2018)

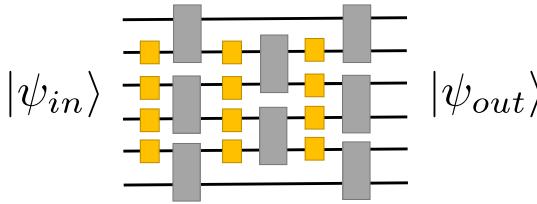
## Exploring latent space



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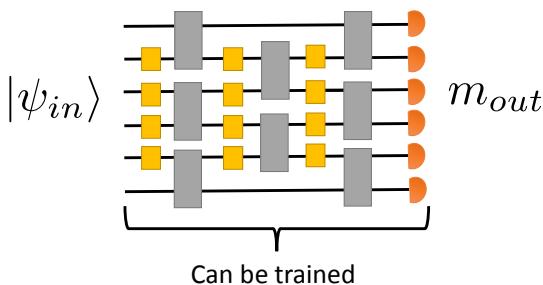
# Training Quantum Circuits

An analogy to machine learning



Define suitable cost functions as expectation values of observables

Optimize them to train quantum circuits for performing quantum tasks

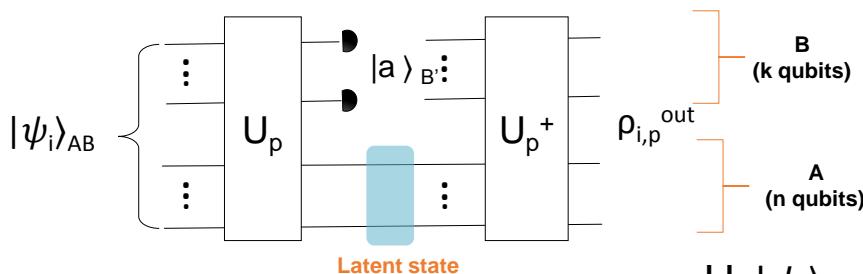


Near-term quantum computers, without error correction and short-depth, are excellent candidates for these *task-driven* applications.

Can be trained

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## Quantum Autoencoder Model



$$U_p |\psi_i\rangle_{AB} = |\psi_i^c\rangle_A |a\rangle_B$$

Given:

- An ensemble of pure states  $\{q_i, |\psi_i\rangle_{AB}\}$  and a pure reference state  $|a\rangle_{B'}$  on  $k$  qubits.
- A family of unitary operators  $\{U_p\}$  acting on  $n+k$  qubits, parameterized according to a parameter vector  $\mathbf{p} = (p_1, p_2, \dots)$ .

Task:

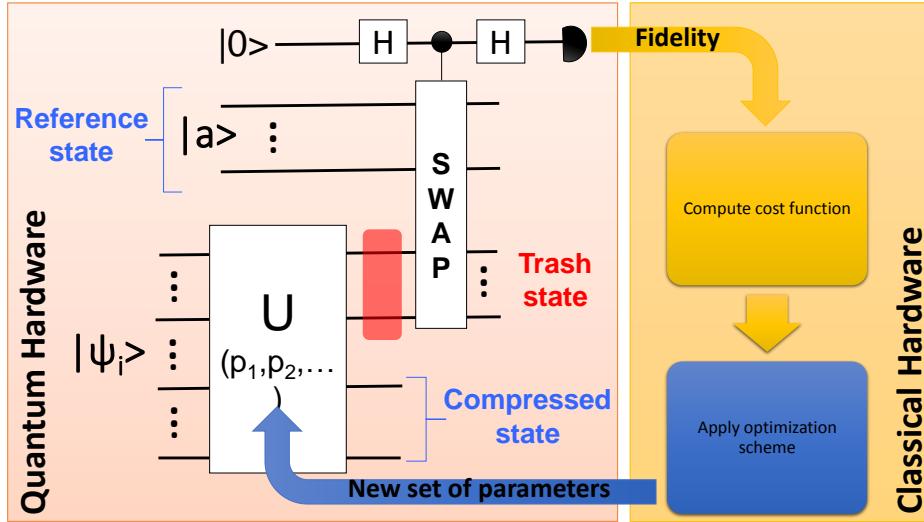
- Find the unitary  $U_p$  which maximizes:  $C(p) = \sum_i q_i F(|\psi_i\rangle_{AB}, \rho_{i,p}^{out})$

[Romero, J., Olson, J. and Aspuru-Guzik, A., . Quantum autoencoders for efficient compression of quantum data. \*Quantum Sci. Technol.\* 2 \(2017\): 045001.](#)

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## Hybrid Approach for Circuit Training

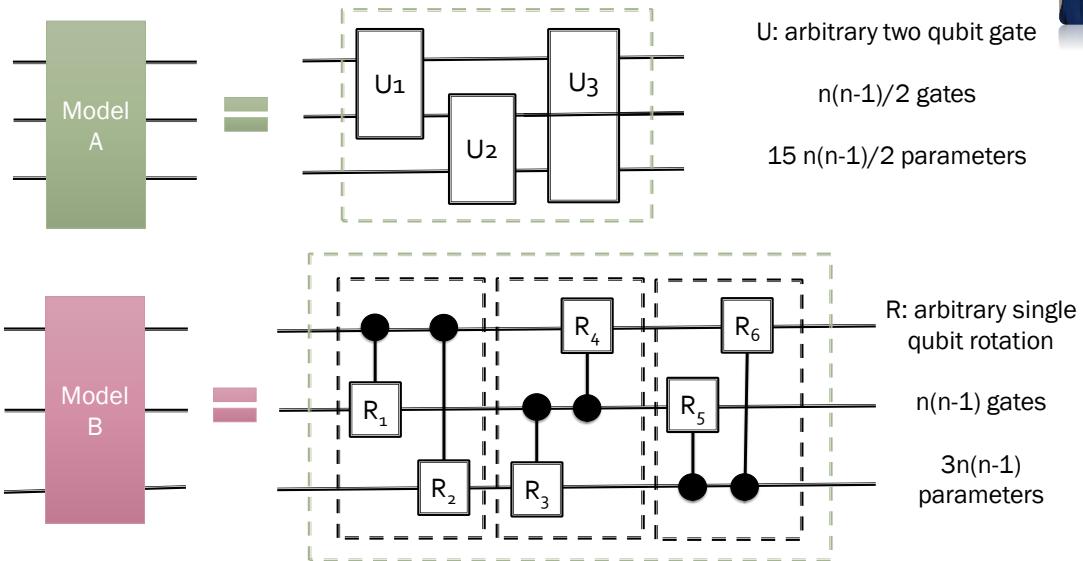


Romero, J., Olson, J. and Aspuru-Guzik, A., 2016. Quantum autoencoders for efficient compression of quantum data. *Quant Sci Tech* 2 045011 (2017)

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## Heuristics for Autoencoder Unitaries



Romero, J., Olson, J. and Aspuru-Guzik, A., 2016. Quantum autoencoders for efficient compression of quantum data. *Quant Sci Tech* 2 045011 (2017)

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# Application: Wave Function Compression

Romero, et al *Quant Sci Tech* 2 045011 (2017)



For many Hamiltonians, eigenstates are generally sparse and obey certain symmetries.

Example: In many body systems there are

**Restriction in the number of particles:** with  $m$  particles within a second quantized representation, wavefunctions are spanned by a subspace of size  $\binom{N}{m}$ , compared to  $2^N$ .

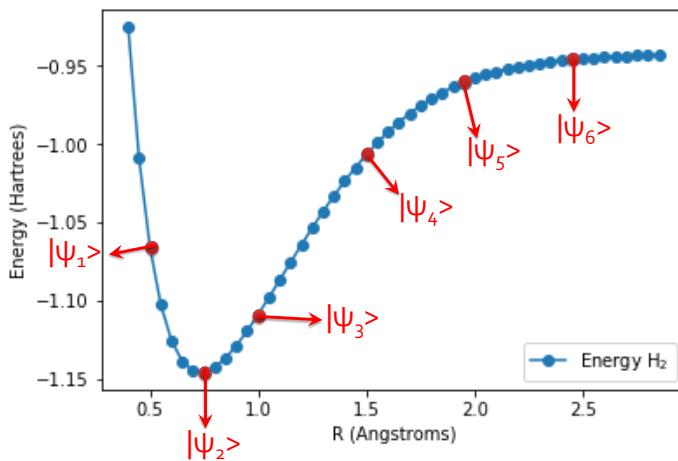
**Restriction in spin projection:** The total wavefunction is spanned by determinants with the correct spin projection:

$$S_z|k\rangle = M|k\rangle; \quad M = \frac{n_\alpha - n_\beta}{2}$$

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## Example: H<sub>2</sub> molecule (4-2-4 autoencoder)

Romero, et al *Quant Sci Tech* 2 045011 (2017)



- We selected some points in the PES for which we have the wavefunction (Use VQE as oracle).
- Use these states as training set for the autoencoder. (6)
- Use other points in the PES as test set. (44)

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# H<sub>2</sub> Results

Romero, et al arXiv:1612.02806



Circuit	Final size (# qubits)	Set	$-\log_{10}(1 - \mathcal{F})$	$-\log_{10}$ Energy
			MAE	MAE (Hartrees)
Model A	2	Training	6.96(6.82-7.17)	6.64(6.27-7.06)
	2	Testing	6.99(6.81-7.21)	6.76(6.18-7.10)
	1	Training	6.92(6.80-7.07)	6.60(6.23-7.05)
	1	Testing	6.96(6.77-7.08)	6.72(6.15-7.05)
Model B	2	Training	6.11(5.94-6.21)	6.00(5.78-6.21)
	2	Testing	6.07(5.91-6.21)	6.03(5.70-6.21)
	1	Training	3.95(3.53-5.24)	3.74(3.38-4.57)
	1	Testing	3.81(3.50-5.38)	3.62(3.35-4.65)

\* MAE: Mean Absolute Error. Log chemical accuracy in Hartrees  $\approx -2.80$

Average error in the fidelity after one cycle of compression and decompression using the quantum autoencoder trained from ground states of the Hydrogen molecule

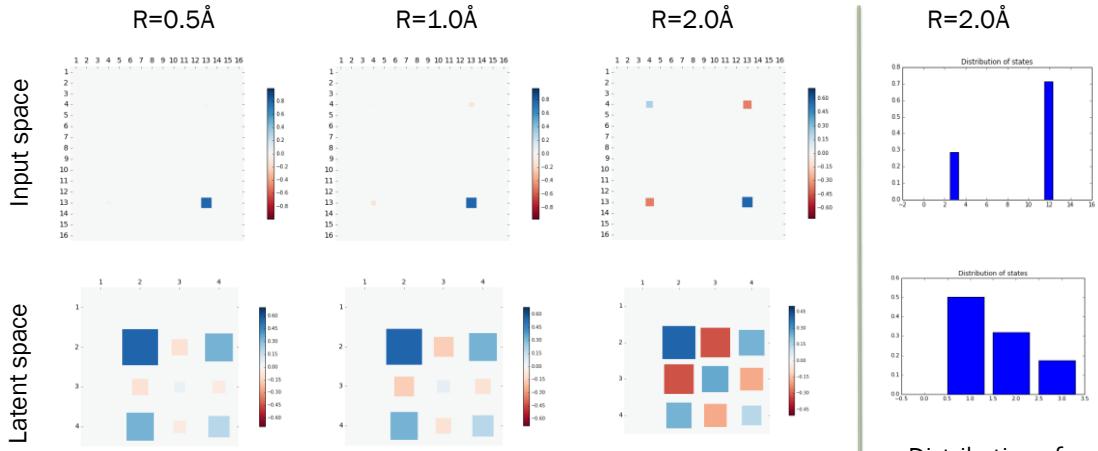
87

# Compressed H<sub>2</sub>

Romero, et al Quant Sci Tech 2 045011 (2017)



- Average fidelity in training set: 0.9895 - Average fidelity in testing set: 0.9873



Density matrices of the input and latent spaces at different distances

Distribution of states at R=2.0 Å

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Twitter alert at 9:28 AM!

Rigetti Computing  
@rigetti

Follow

QCompress is a simulation tool for the quantum autoencoder that compresses and recovers quantum data. Read more in our latest guest post by Hannah Sim from the @ZapataComputing team.

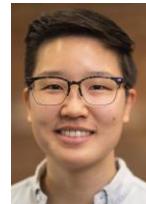
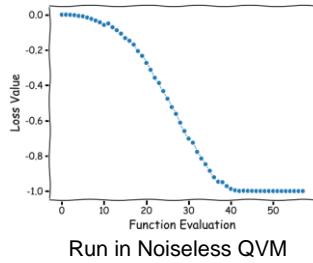
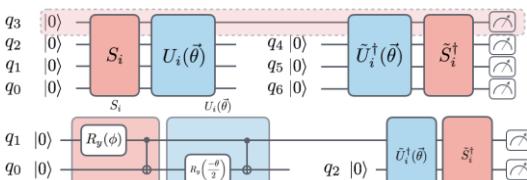
**QCompress: Implementation of the Quantum Autoencoder ...**

By Sukin (Hannah) Sim  
medium.com

9:28 AM - 30 Jul 2018

<https://medium.com/rigetti/qcompress-implementation-of-the-quantum-autoencoder-using-forest-and-openfermion-7f99f7e45ff8> 89

## Experiment!: H<sub>2</sub> molecule (4-1-4, 2-1-2 autoencoder)

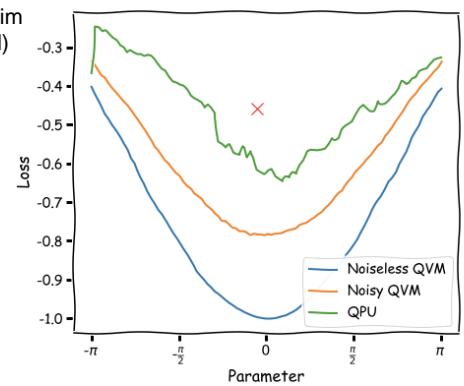


Hannah Sim  
(Harvard)

Rigetti Computing Follow  
On a mission to build the world's most powerful computer.  
Jul 30 · 5 min read

### QCompress: Implementation of the Quantum Autoencoder using Forest and OpenFermion

By Sukin (Hannah) Sim



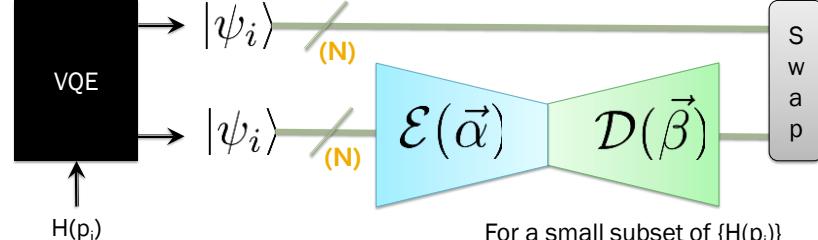
<https://medium.com/rigetti/qcompress-implementation-of-the-quantum-autoencoder-using-forest-and-openfermion-7f99f7e45ff8>

90

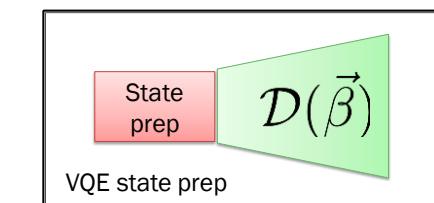
# CUSP (Zapata Computing + Google) Autoencoder + Variational eigensolver



For a family of Hamiltonians  
 $\{H(p_i)\}$   
 $i=1, \dots, M$



The purpose  
is to reduce  
the number  
of  
parameters  
for the state  
preparation



For a small subset of  $\{H(p_i)\}$

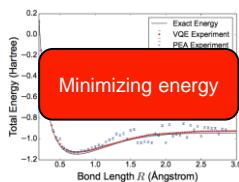
For the remaining  $\{H(p_i)\}$

91

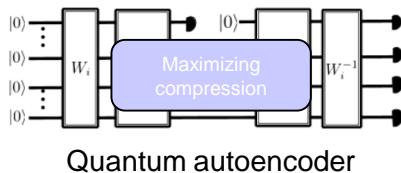
## The age of variational quantum algorithms ... training quantum circuits.



### Variational quantum eigensolver



Peruzzo et al. (2014)



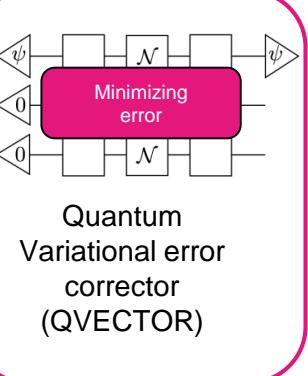
Romero, et al.  
Quantum Sci. Technol. 2 (2017): 045001

Quantum adiabatic optimization  
Maximizing cut size algorithm  
Farhi et al. (2014)



Cao, et al.  
arXiv:1711.11240

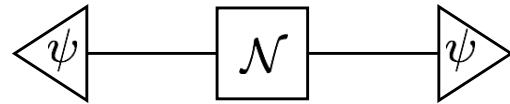
Quantum neuron



... and many other algorithms, e.g. Machine Learning

92

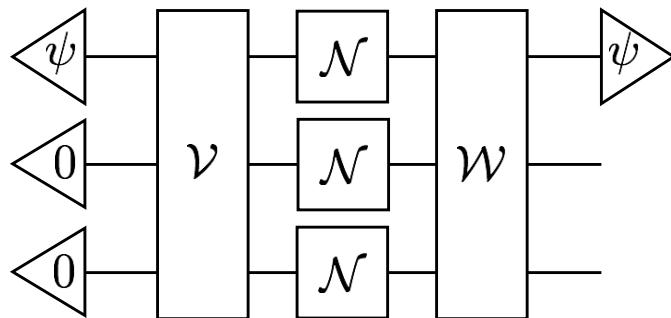
# Quantum Error Correction in a Nutshell



$$\mathcal{F}_{\text{avg}} = \int d\psi \sum_i \langle \psi | N_i | \psi \rangle \langle \psi | N_i^\dagger | \psi \rangle$$

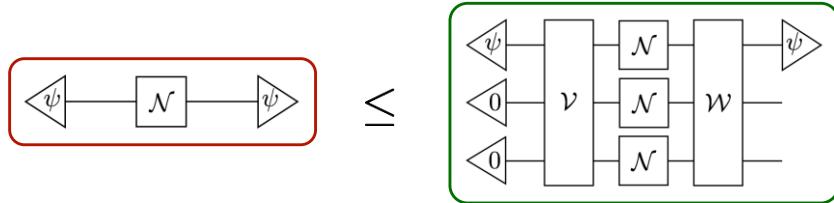
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# Quantum Error Correction in a Nutshell



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# Quantum Error Correction in a Nutshell



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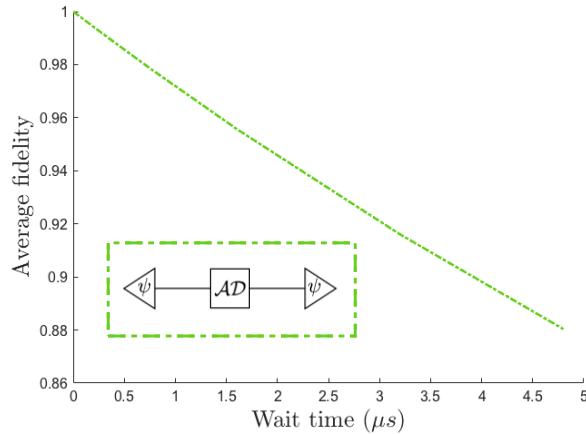
# Quantum Error Correction in a Nutshell



*What is the quality of error correction for this process?*

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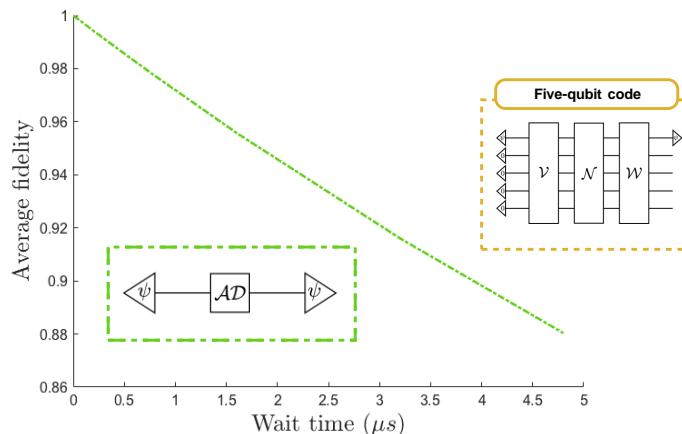
# Single Qubit Decoherence



$$T_2 = 60\mu s = T_1/3$$

97

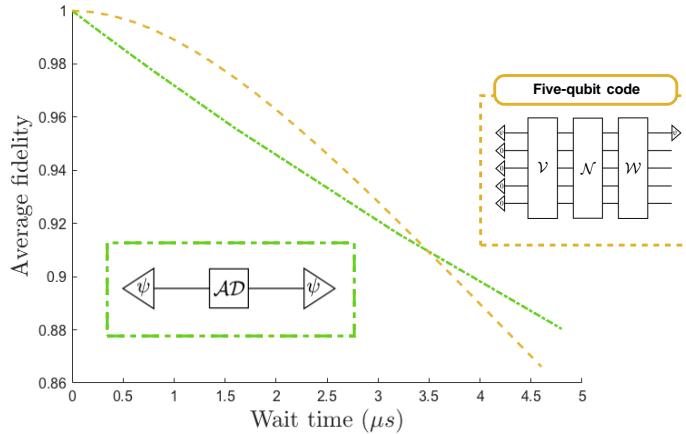
# Single Qubit Decoherence



$$T_2 = 60\mu s = T_1/3$$

98

## Encode-Wait-Decode for 5-Qubit Stabilizer Code



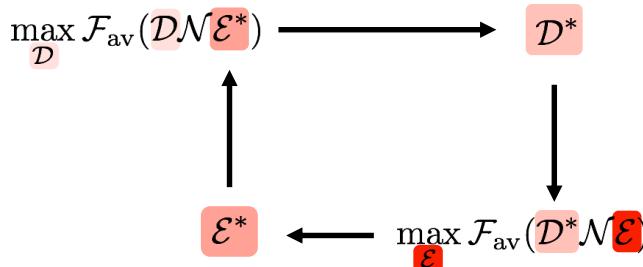
$$T_2 = 60\mu s = T_1/3$$

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## Bi-convex Optimization of Average Fidelity

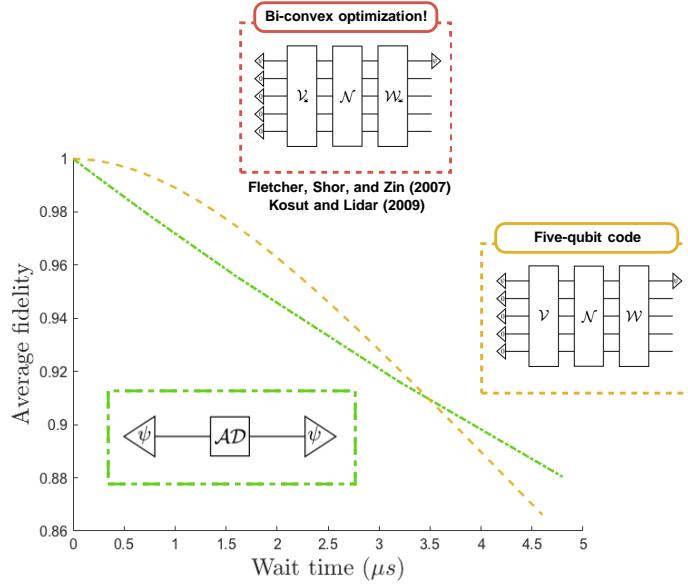


- 1) Solve SDP for optimal decoding
- 2) Plug in optimized decoding
- 3) Solve SDP for optimal encoding
- 4) Plug in optimized encoding
- 5) Repeat 1-4 until sufficient convergence of average fidelity



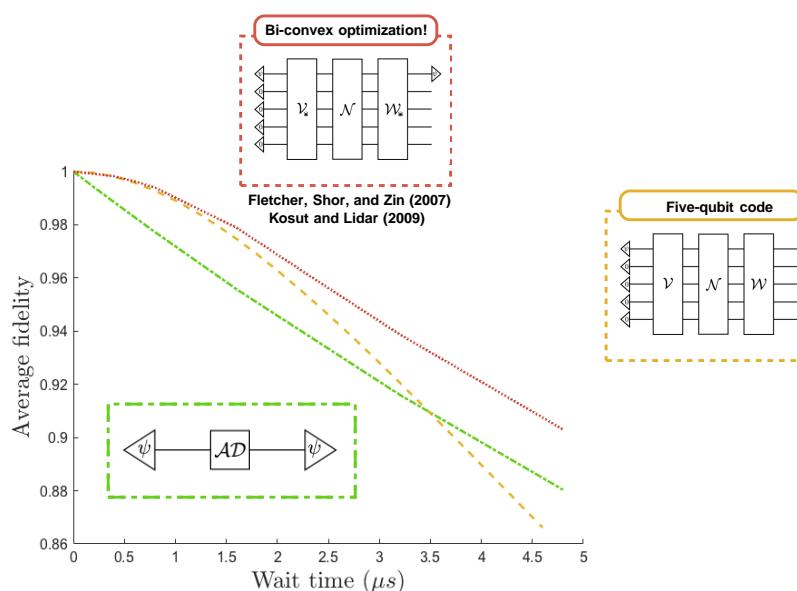
Fletcher, Shor, and Zin (2007)      Kosut and Lidar (2009)

100



$$T_2 = 60\mu s = T_1/3$$

101



$$T_2 = 60\mu s = T_1/3$$

102



## Previous Approaches

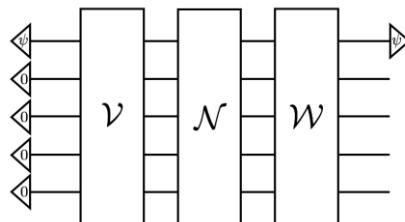
1. Require noise model
2. Optimization unscalable
3. Gate compilation needed

## Our Algorithm (QVECTOR)

- Model Free
- Efficient Evaluation
- Built-in Gate Decomposition

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## Quantum Variational Error CorrecTOR

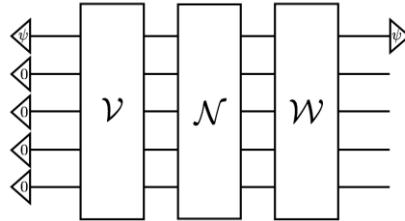


Variational quantum optimization algorithm for designing quantum error correcting schemes...

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## QVECTOR



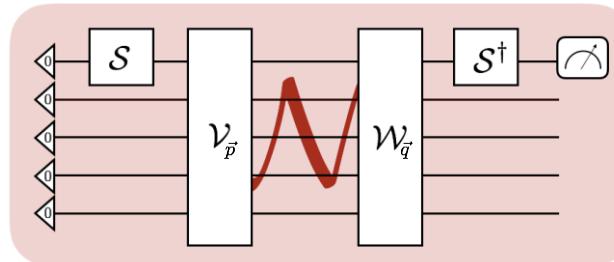
Variational quantum optimization algorithm for designing quantum error correcting schemes...

*Objective: maximize average fidelity*

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## Model Free



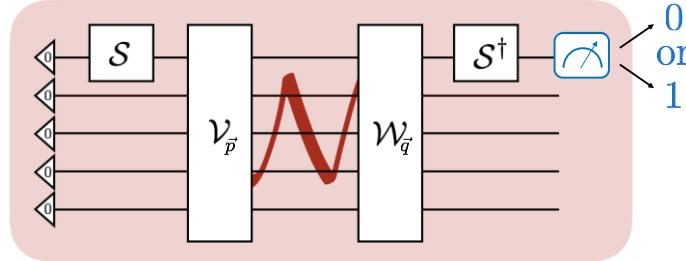
*In situ* optimization...

... noise “perfectly” simulates itself.

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## Efficient Evaluation



$N$  random samples  $\mathcal{S}$  (from 2-design)

Fraction of 0-outcomes estimates average fidelity to  $\mathcal{O}(1/\sqrt{N})$ .

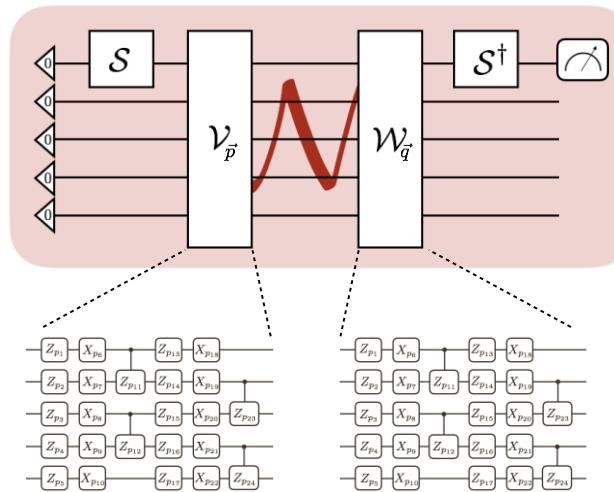
2-design samples from Clifford group instead of Haar-random unitaries

Dankert et al. (2009)

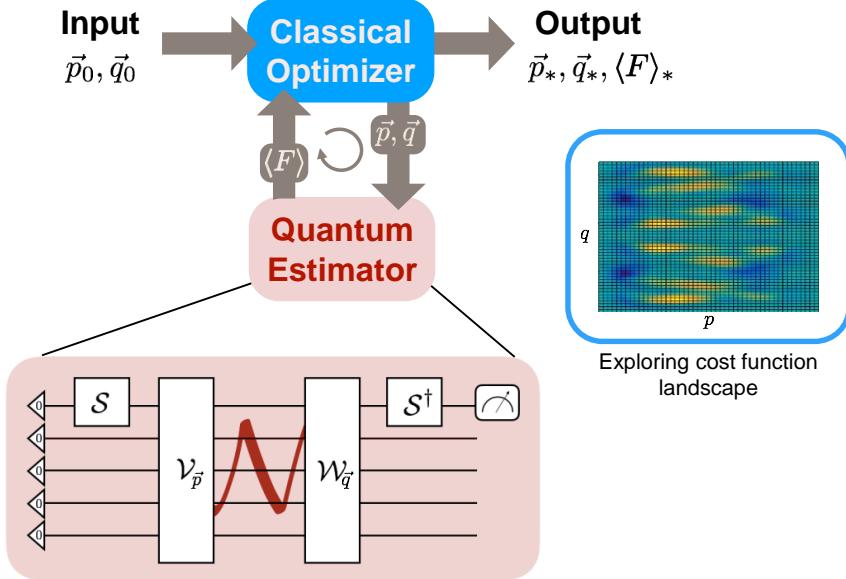
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## Built-in gate decomposition



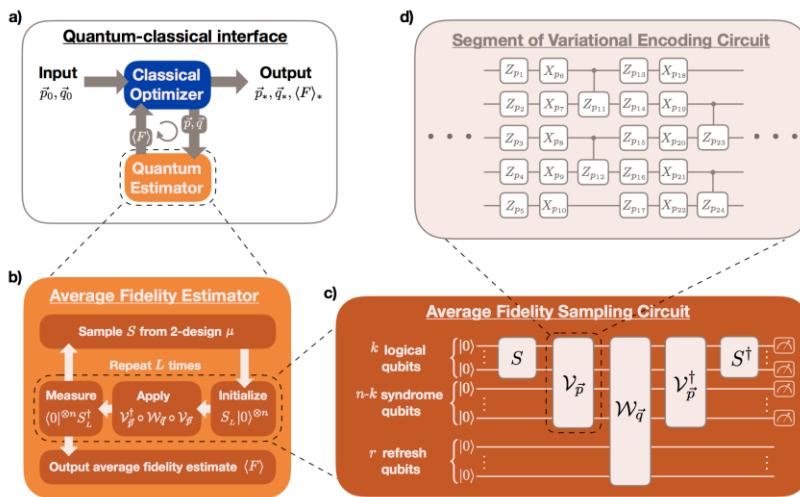
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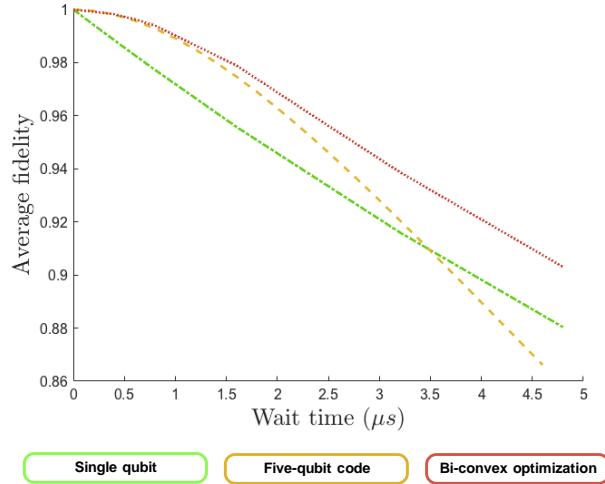
109



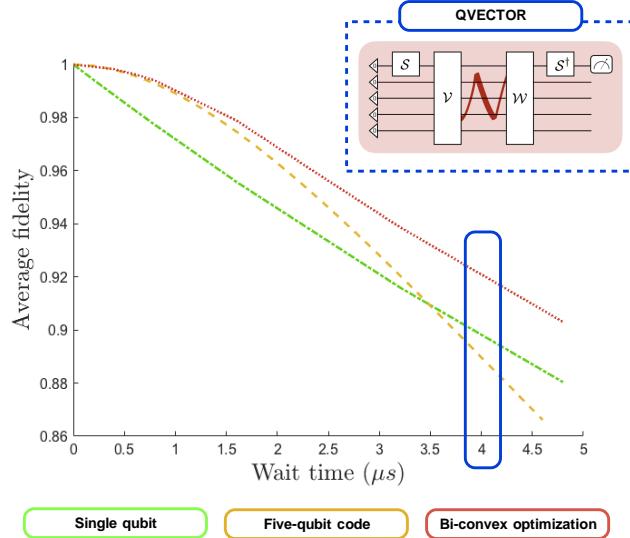
## QVECTOR Schematic



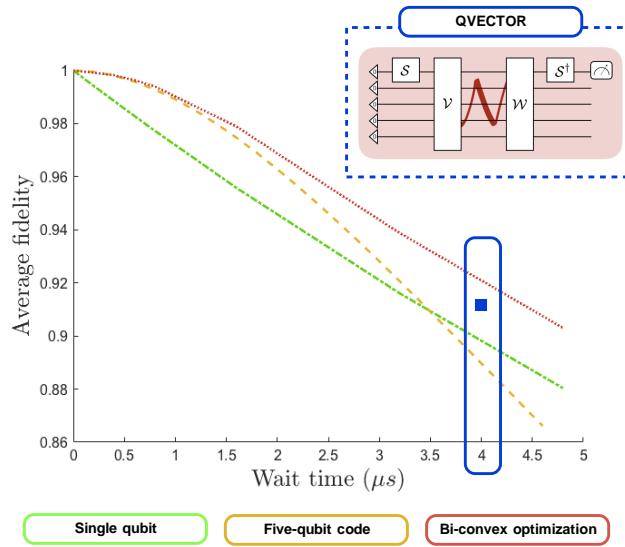
110



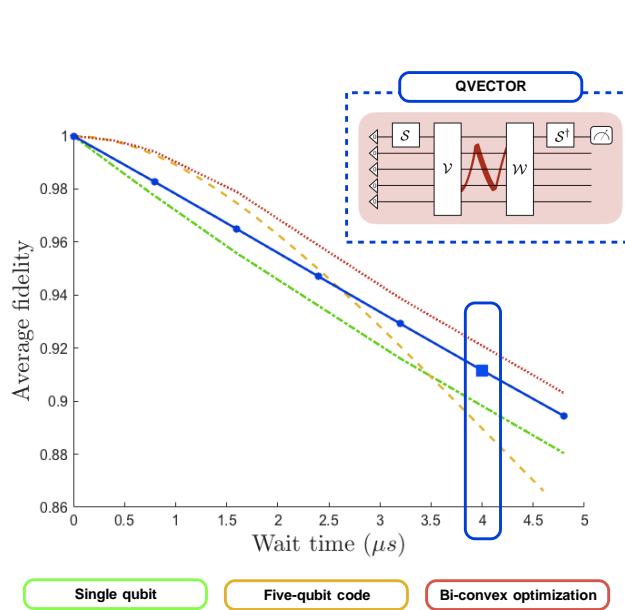
111



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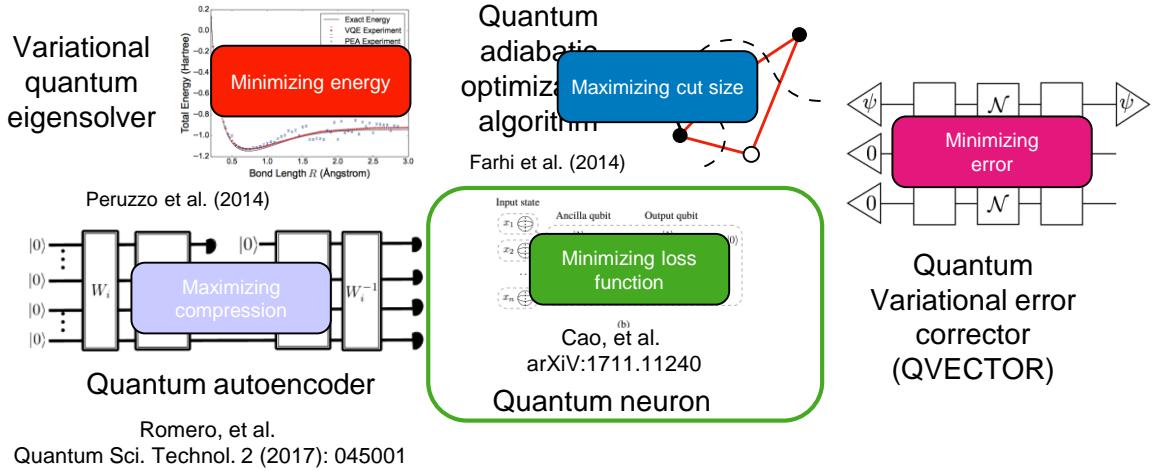


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## The age of variational quantum algorithms ... training quantum circuits.



Romero, et al.  
Quantum Sci. Technol. 2 (2017): 045001

... and many other algorithms, e.g. Machine Learning

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## Basic requirements for quantum NN



1. Initial state encodes any  $N$ -bit binary string  $01001 \rightarrow |01001\rangle$
2. Reflects one or more basic neural computing mechanisms e.g. attractor dynamics, synaptic connections, integrate & fire, training rules, structure of a NN
3. The evolution is based on quantum effects Superposition and entanglement

Schuld, M., Sinayskiy, I. & Petruccione, F. *Quantum Inf Process* (2014) 13: 2567

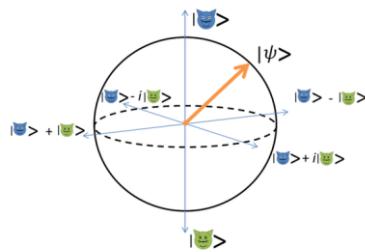
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# QM + NN: an unlikely match ?



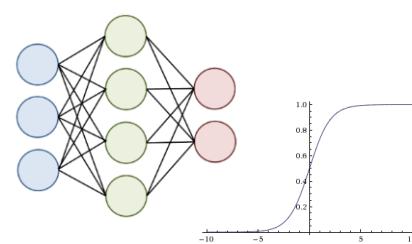
## Quantum Mechanics (QM)

- Unitary evolution
- Rotation in Hilbert space



## Neural Networks (NN)

- Lossy transformations
- Clustering, classification, compression etc



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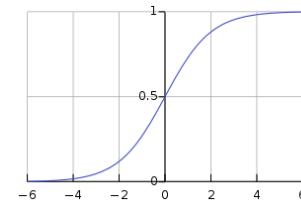
# Challenges



- Sigmoid / step function activation

How to realize on quantum computers,  
whose dynamics is linear?

Reversible circuits  
Dissipative dynamics



- Measurement? Open system?

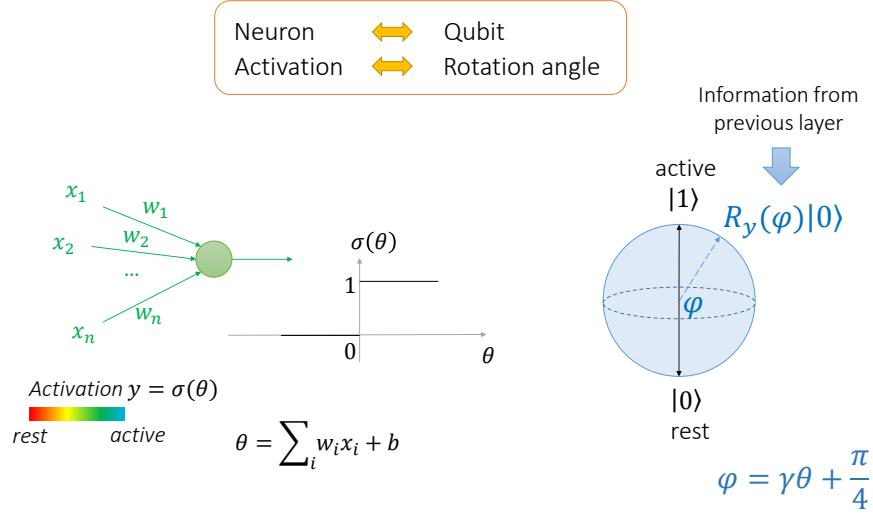
May collapse the state / reduce to  
classical probabilistic algorithms

Story of quantum error correction

Cost scaling?

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# Our Proposal



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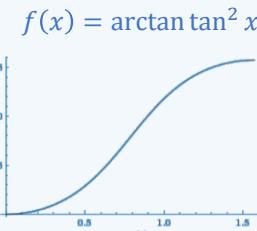
## Introduce Nonlinearity



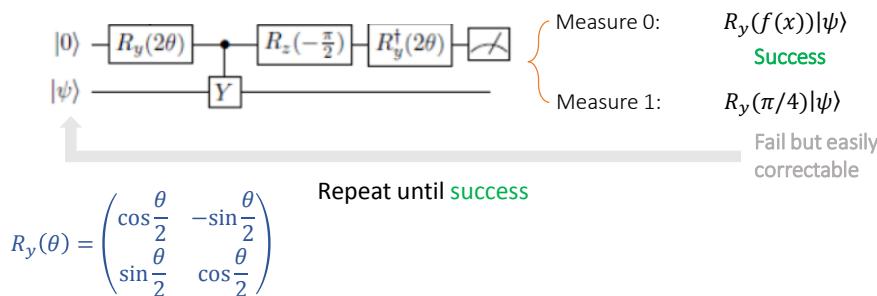
Repeat-until-success (RUS) circuits:

Given ability to realize  $R_y(2x)$

One could use RUS to realize  $R_y(2f(x))$



Nonlinear!

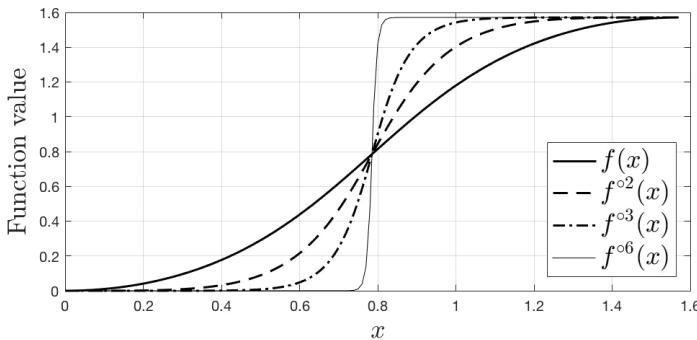


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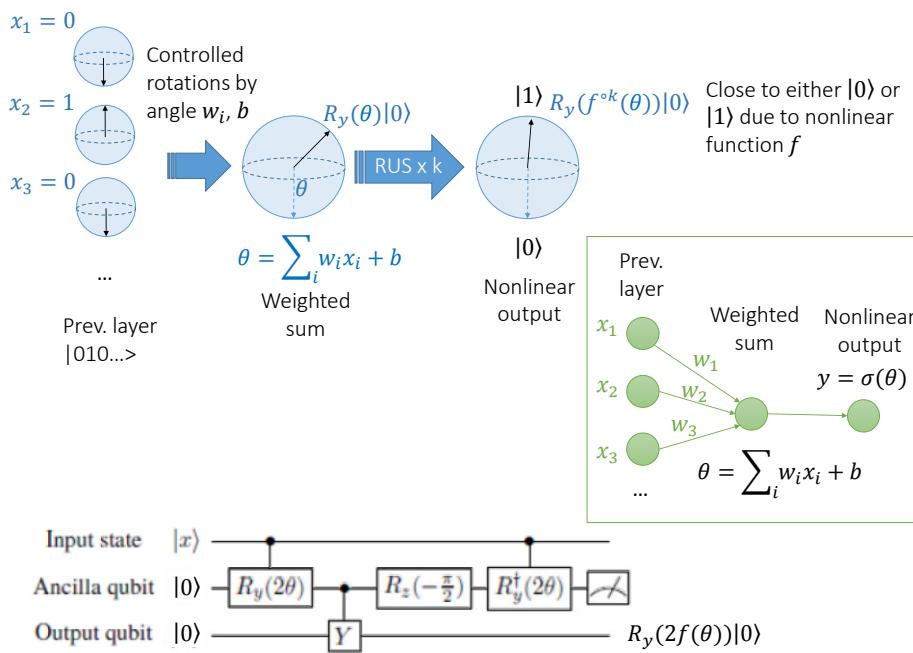
$$R_y(x) \rightarrow R_y(f(x)) \rightarrow \dots \rightarrow R_y(f^{\circ k}(x))$$



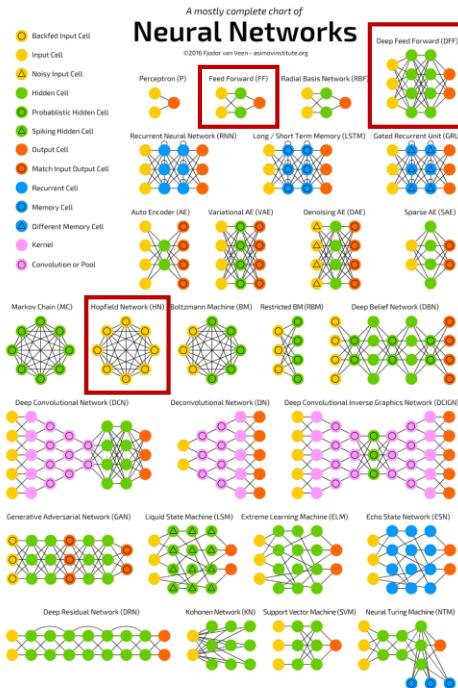
$$\underbrace{f(f(\dots f(x) \dots))}_{k \text{ times}} = f^{\circ k}(x)$$



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- Size
- Neuron type
- Connectivity
- Activation function
- Weight/bias setting
- Training method
- ...

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### Hopfield Network (HN)

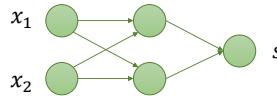
#### Feed Forward (FF)



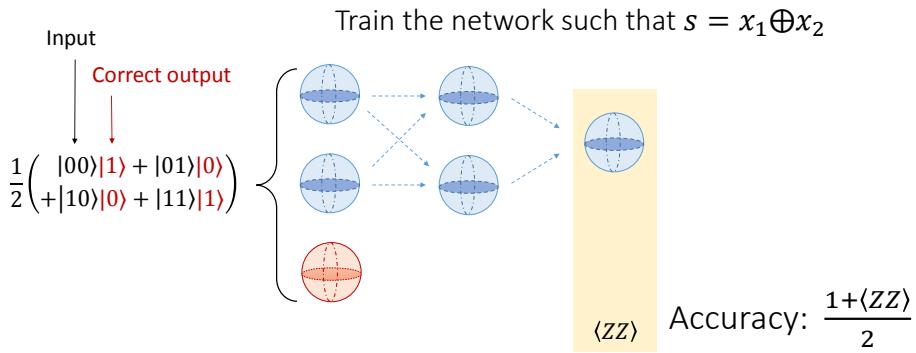
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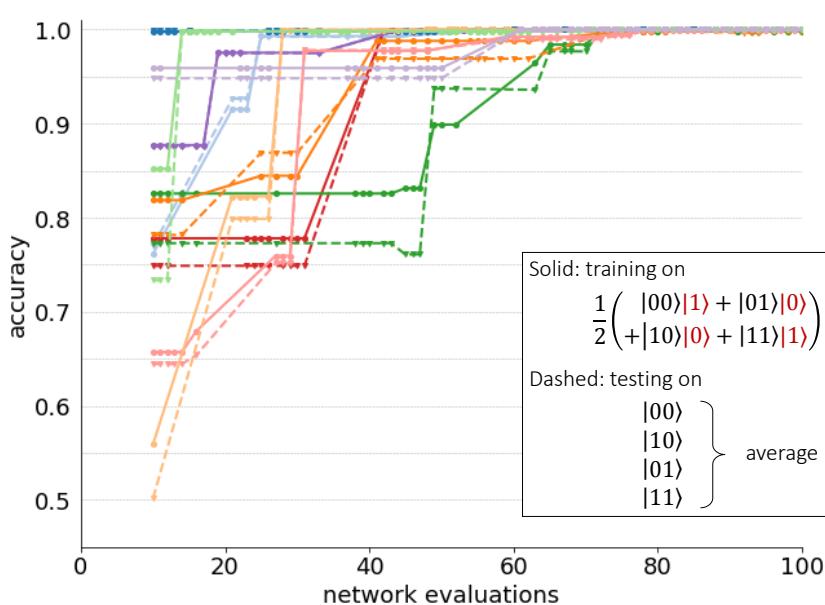
# XOR Network



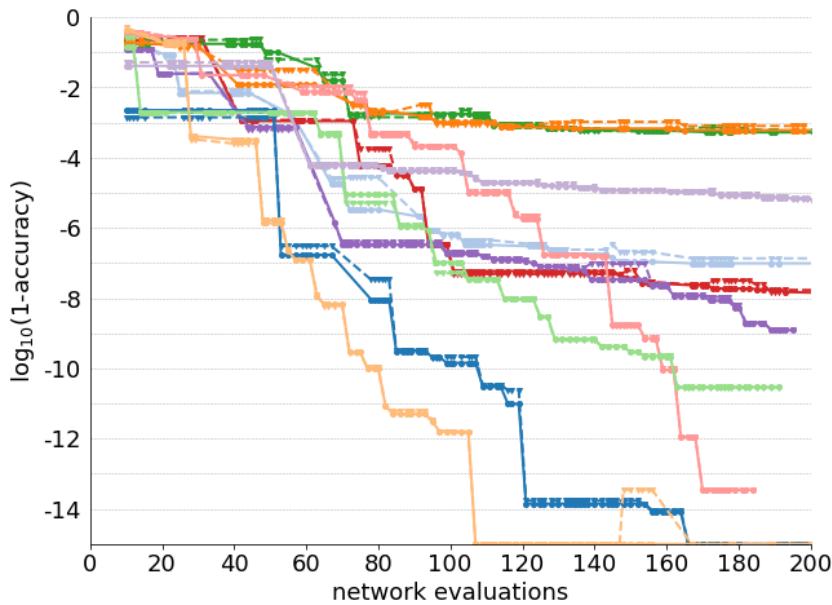
$x_1$	$x_2$	$s$
0	0	0
0	1	1
1	0	1
1	1	0



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## Summary



- Building block for quantum neural network satisfying
  - Initial state encoding  $n$ -bit strings  
*Neuron <-> Qubit*
  - One or more neural computing mechanisms  
*Sigmoid/step function, attractor*
  - Evolution based on quantum effects  
*Train with superposition of examples*
- Application and extensions
  - Superposition of weights (networks) ?
  - Different forms of networks
  - Different activation functions

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Enter the quantum software era.

How about a *platform neutral*, near-term focused quantum software startup?

Look no further!



**Zapata**Computing

Email: [info@zapatacomputing.com](mailto:info@zapatacomputing.com)

# Z is the new Q

## Collaborators



Jonathan Romero



Jonathan  
Olson



Hanna Sim



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Dallaire-Demers  
(Now at Xanadu)

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Ville Bergholm (ISI)  
Dominic Berry (McQuarrie)  
Sergio Boixo (Google)  
Jacob Biamonte (Skolkovo)  
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Ivan Kassal (Sydney)  
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Enrique Solano (UPV)

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Bryan O'Gorman (NASA)  
Peter O'Malley (Google)  
Borja Peropadre (BBN)  
Nicolas Sawaya (Intel)  
Mikhail Smelyanskiy (Facebook)  
Dave Wecker (Microsoft)  
Annie Wei (MIT)  
Jonathan Welch  
James Whitfield (Dartmouth)  
Andrew White (Queensland)  
Nathan Wiebe (Microsoft)  
Jörg Wrachtrup (Stuttgart)  
Man-Hong Yung (Tsinghua)  
Yoshi Yamamoto (Stanford)

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Ian Kivlichan  
Mattias DeGroote  
Jonny Olson  
Tim Menke  
Jonathan Romero  
Hannah Sim

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## Aspuru-Guzik Group

<http://matter.toronto.edu>

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NSF, ARO, ONR, AFOSR, Sloan Foundation, Camille and Henry  
Dreyfus Foundation, DTRA, DARPA, Anders Froseth



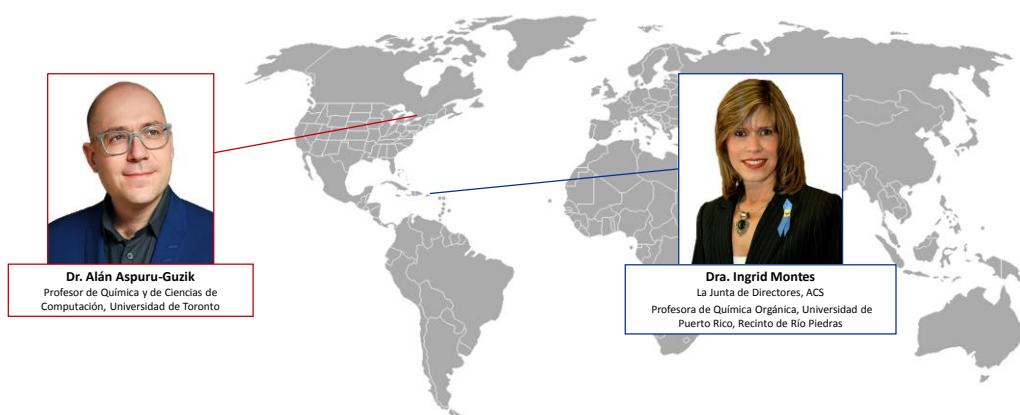
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### “Cómputo Cuántico para Química”



**Dr. Alán Aspuru-Guzik**  
Profesor de Química y de Ciencias de  
Computación, Universidad de Toronto

**Dra. Ingrid Montes**  
La Junta de Directores, ACS  
Profesora de Química Orgánica, Universidad de  
Puerto Rico, Recinto de Río Piedras

*Las imágenes de la presentación están disponibles para descargar ahora desde el panel de GoToWebinar*  
<http://bit.ly/ComputoCuantico>

El Webinar de hoy está auspiciado por la Sociedad Química de México y the American Chemical Society

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Hoy tenemos representantes de **24 países**

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## ¡C&EN en Español!

C&EN pone a su disposición traducciones al español de sus artículos más populares.

August 14, 2018

**La FDA aprueba la primera terapia con ARN interferente**  
El fármaco Onpattro pone fin a dos décadas de trabajo académico e industrial para llevar los ARN interferentes al mercado farmacéutico.



**FDA approves first-ever RNAi therapeutic**

Nostrum Farmaceuticos ha llevado dos décadas de trabajo académico e industrial para llevar los ARN interferentes al mercado farmacéutico.

July 31, 2018

**El óxido nítrico del permafrost tibetano esconde malas noticias para el calentamiento global**  
Los científicos estiman que el deshielo podría liberar grandes cantidades de este gas de efecto invernadero.



**Nitrous oxide from Tibetan permafrost packs global warming punch**  
Los científicos estiman que el deshielo podría liberar grandes cantidades de este gas de efecto invernadero.

July 25, 2018

**Peces sin olfato en los océanos acidificados**  
Los crecientes niveles de CO<sub>2</sub> podrían impedir que los peces encuentren comida o detecten sus depredadores.



**Fish struggle to smell in acidic oceans**

Rising CO<sub>2</sub> levels could stop fish finding food and detecting predators.

Gracias a una colaboración con la organización española Divulgame.org, C&EN ahora es capaz de ofrecer traducciones al español de algunos de nuestros mejores contenidos. Queremos hacer de la ciencia de vanguardia más accesible a la comunidad química de habla española, y esta es nuestra contribución. Le da a los nacidos en España, América Latina, o los EE.UU., pero cuyo primer idioma es el español la oportunidad de leer este contenido en su lengua materna. Esperamos que les guste y sea de su utilidad.



**Dr. Bibiana Campos Seijo**  
Editora en Jefe, C&EN

<http://bit.ly/CENespanol>

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## Sociedad Química de México



Desde sus comienzos de la Sociedad Química de México, se buscaba un emblema sencillo, no demostrar partidismo alguno y significar al gremio, debería representar un símbolo no sólo para los químicos, sino también para ingenieros, farmacéuticos, metalurgistas, en fin que englobe e identifique por igual a los científicos en todas sus áreas de las ciencias químicas.

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